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Implementing a menu of options in decumulation-only CDC plans

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www.actuaries.org.uk/arc



Research programme: “Optimising future pension plans”

- Pooled annuity funds
 - Type of CDC scheme.
 - Decumulation-only.
 - Pool longevity risk only, no investment risk-sharing.
- Collective defined contribution (CDC) schemes.
- Outputs: <https://www.actuaries.org.uk/learn-and-develop/research-and-knowledge/actuarial-research-centre-arc/current-research/optimising-future-pension-plans-phase-ii>



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Today's talk

- Why pooled annuity funds?
- What must they be able to do?
- Investment strategies.
- Joint life benefits.



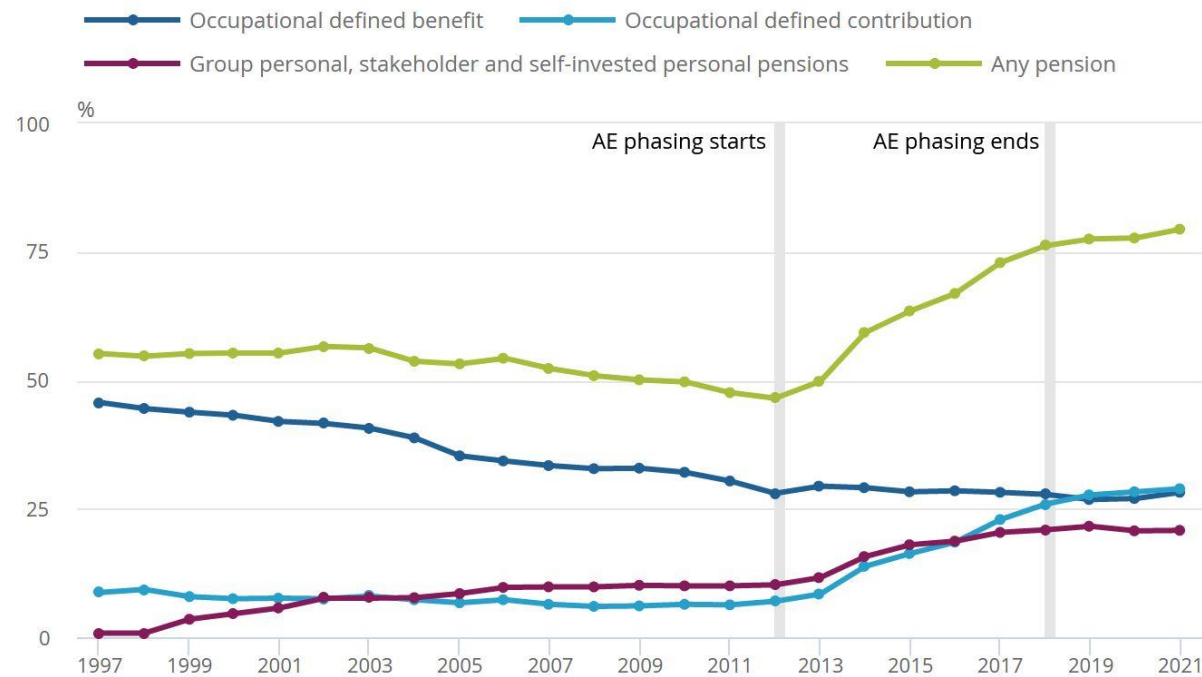
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Current situation – ONS data

- 22.6 million workers saving into work-place pension.

Proportion of employees with workplace pension by type of pension, UK,
1997 to 2021



What do people want financially in retirement?

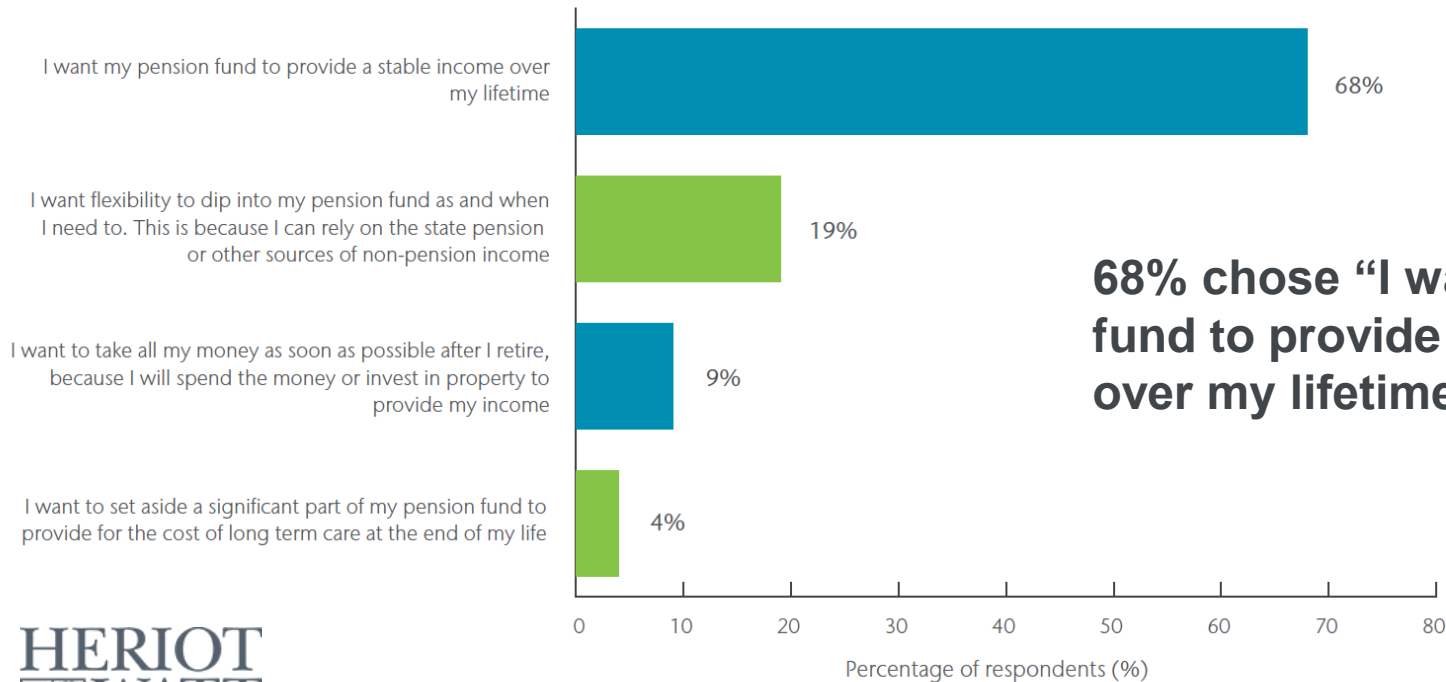
In a brave new pensions world what will DC members really want?

Chart 9 – Using retirement savings

Which of the following statements best describes your attitude towards how you might spend your pension fund?

Aon DC Member Survey

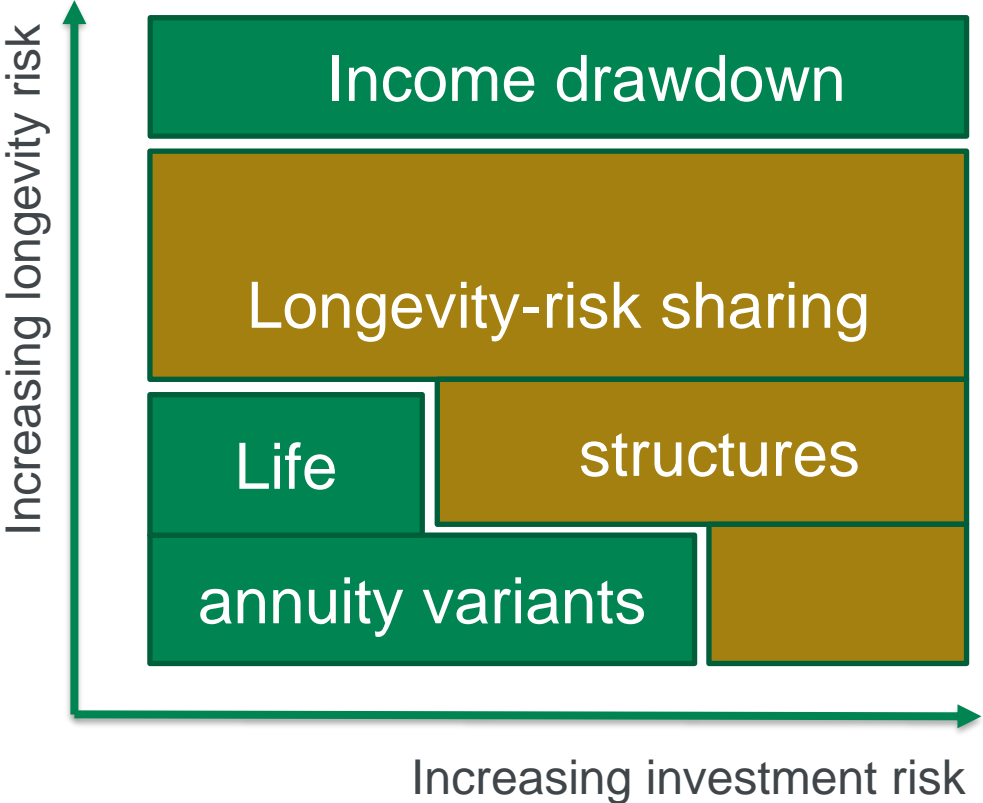
Aon Hewitt and Cass Business School
London, December 2014



Are pooled annuity funds the answer?

- Pooled annuity fund:
 - Join at retirement with lump-sum contribution.
 - Paid a lifelong income in retirement.
 - Earn investment returns + longevity credits
- Sharing longevity risk makes a lot of sense.
 - Don't have to guess for how many years you will live...
 - ...Reduce significantly/eliminate idiosyncratic risk.
 - Still left with systematic longevity risk...
 - But overall have a reduction in longevity risk.

Decumulation options



Summary of data

- Typical DC pension saver:
 - Works in the private sector.
 - Has a small amount of DC pension savings.
- If pooled annuity funds are the answer, what must they be able to do?
 - Offer joint life benefits.
 - Perhaps offer a choice of investment funds.
 - Perceived value-for-money, e.g. death benefit reflecting return of funds less income received.
 - Plus...



Real-world examples of pooled annuity funds



Key features of a Lifetime Pension

-  Fortnightly payments for life
-  Spouse protection option
-  Potential Age Pension benefits
-  Time to decide if it suits you (six-month cooling-off period)
-  Money-back protection

Longevity[®]
by Purpose

Longevity Pension Fund

Fund Overview

Income Policy & Distributions

How to Invest

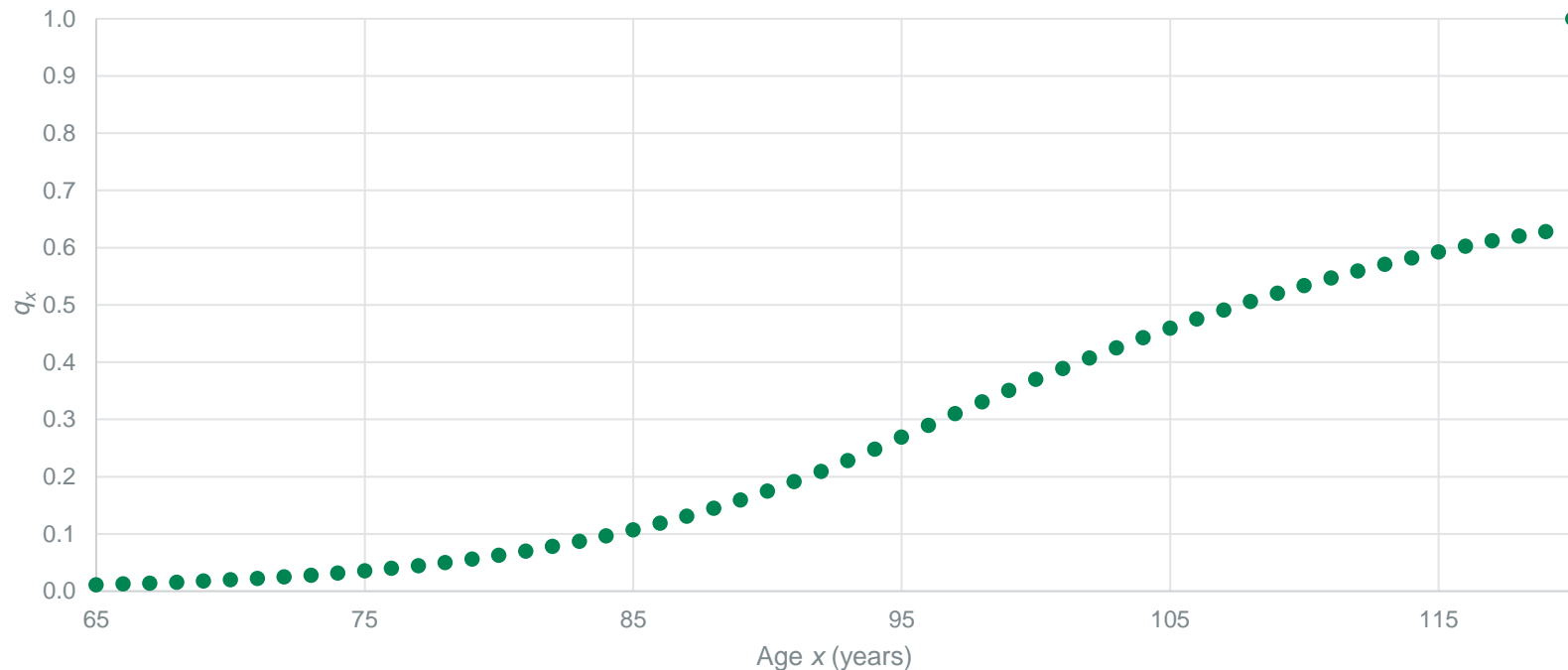
Retire confidently with income for life

The Longevity Pension Fund is a mutual fund trusted by experts

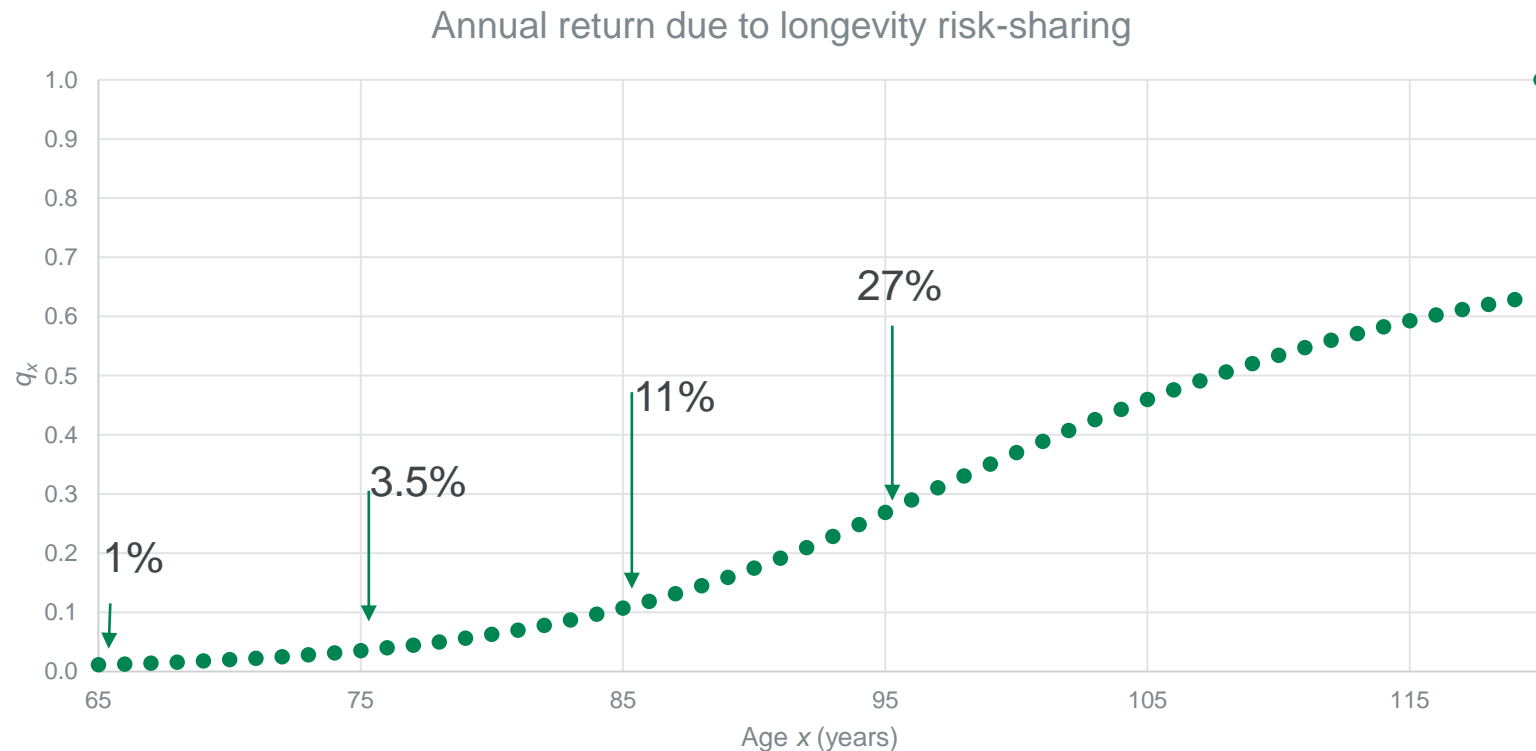
Financial
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Calculations based on UK mortality table S1PMA

Annual probability of death for table S1PMA



Additional return due to longevity risk-sharing



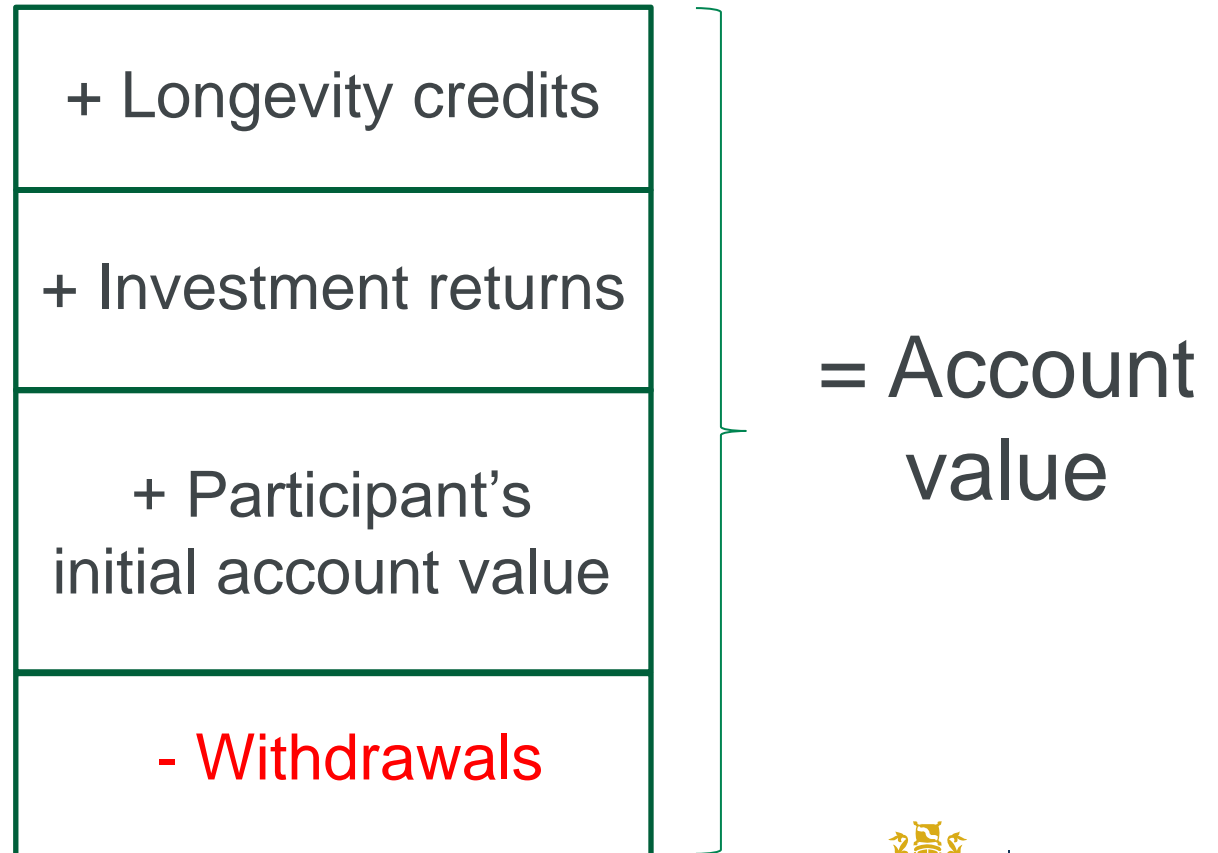
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What is a pooled annuity fund?

- Structure to pool longevity risk and pay regular income for life.
- Everyone becomes the beneficiary of each other.
- Why?
 - To get a higher and life-long income, compared to income drawdown.
 - To get a higher expected income, compared to a life annuity.

Account structure



A certain income profile

- An individual retires at age 65 with £100.
- Invest the £100 in line with a chosen investment strategy.

A certain income profile

- An individual retires at age 65 with £100.
- Invest the £100 in line with a chosen investment strategy.
- Withdraw a constant, monthly income from age 65 to age 75.
- At age 75, buy a life annuity contract with the residual proceeds.

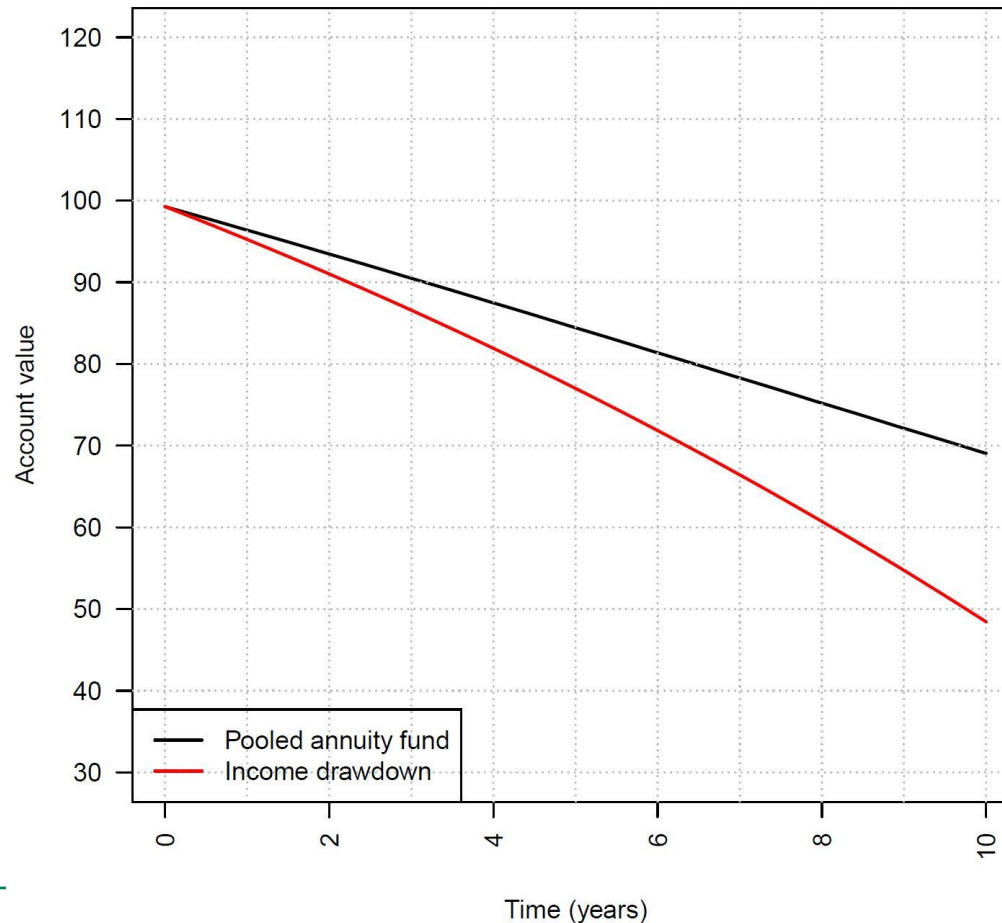
A certain income profile

- An individual retires at age 65 with £100.
- Invest the £100 in line with a chosen investment strategy.
- Withdraw a constant, monthly income from age 65 to age 75.
- At age 75, buy a life annuity contract with the residual proceeds.
- For example, under income drawdown,
 - Invest 100% in risk-free asset earning 5% p.a.
 - Could get an income of ~£6.70 p.a. from age 65 to age 75,
 - Then buy life annuity of ~£5 p.a, paid from age 75.



A certain income profile – development of the £100 account value

Distribution of the account value over time, for pooled annuity fund vs income drawdown, 100% in risk-free asset



Withdraw $\text{£}100/a_{65}^{(12)}$ from age 65 to 75, use residual to buy life annuity income at 75

Annual constant investment return	Which fund gives highest income from age 75?	How much higher than under income drawdown?
2%	Pooled annuity fund	+37%
5%	Pooled annuity fund	+43%
8%	Pooled annuity fund	+50%

The message

- Pooled annuity funds out-perform income drawdown,
 - Due to longevity credits ≥ 0 .
- But note:
 - Comparison is on income only, and
 - Ignores systematic longevity risk.

Improving outcomes

- What investment strategy should the participant in a pooled annuity fund employ?
 - All money in the risk-free asset?
 - Take some investment risk?



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Improving outcomes

- John, 65 years old, starts with £100.
- Could buy a lifetime income of £8.90 per annum at age 65.
- Instead, John withdraws £8.90 p.a. and aims to have a 10% higher income, guaranteed, from age 75.
 - Needs to take investment risk to achieve his goal.
 - The EPV at age 75 of the 10% higher lifetime income is John's target account value.



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Improving outcomes

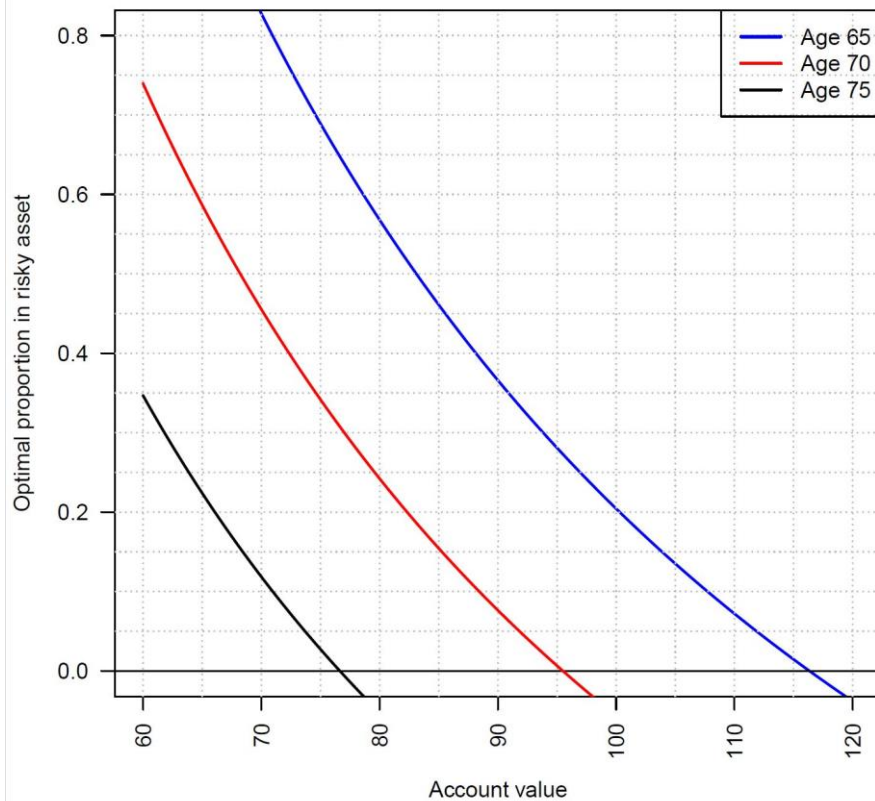
- Assume John wants to minimise how far his account value is from the EPV of his goal.
- Use a quadratic loss function.
- Solve in the Black-Scholes model:
 - A risk-free asset earning a constant risk-free interest rate,
 - A risky asset whose price is driven by a Brownian motion.

Improving outcomes

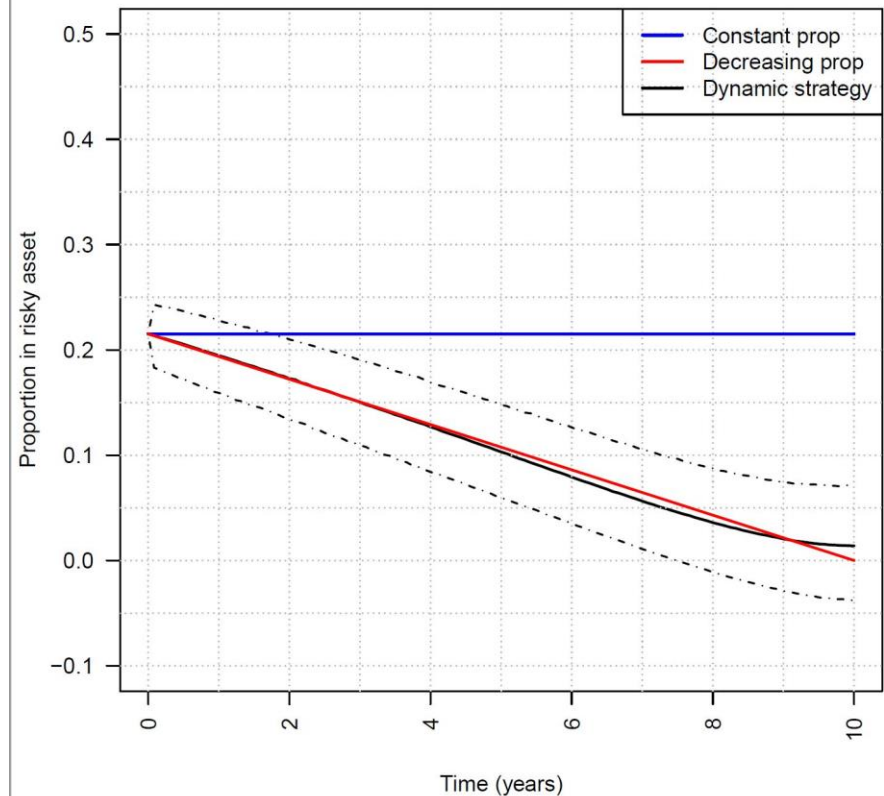
- The solution is a dynamic optimal investment strategy.
- The amount invested in the risky asset changes as John's account value.
 - Invest more in the risky asset, the more that John is below the target.
 - But risk aversion falls over time: John should invest less in the risky asset, the closer he is to age 75.

Improving outcomes: sustainably risk-free income in the first 10 years

Proportion in the risky asset against account value

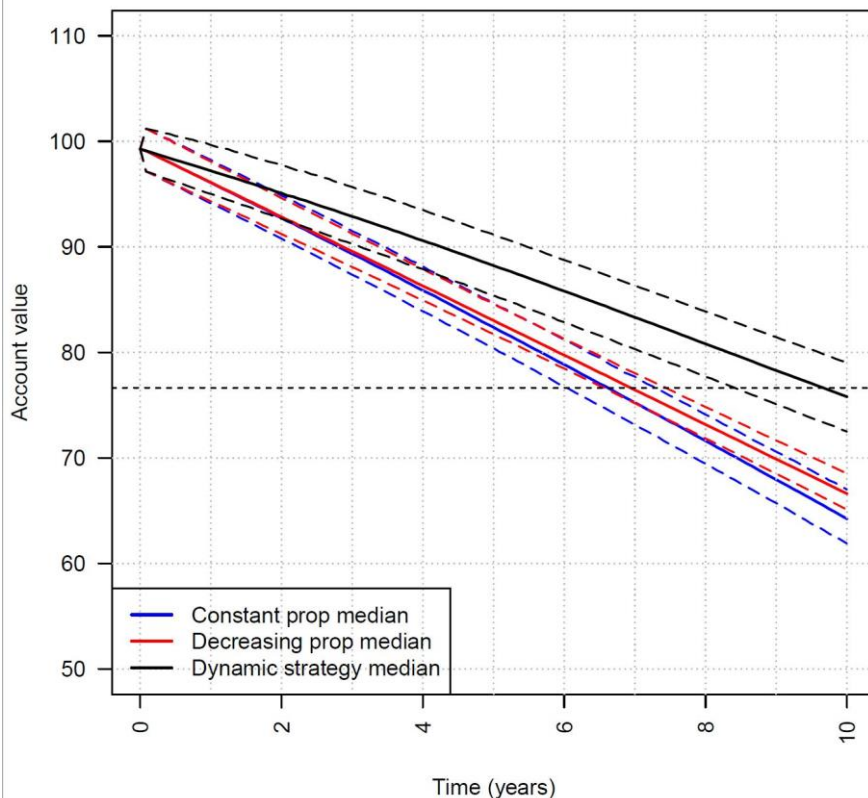


Distribution of proportion in risky asset over time, showing 5th, median and 95th percentiles



Improving outcomes: sustainably risk-free income in the first 10 years

Distribution of the PAF account value over time, showing 5th, median and 95th percentiles



Income bought at age 75 is higher under the dynamic strategy:

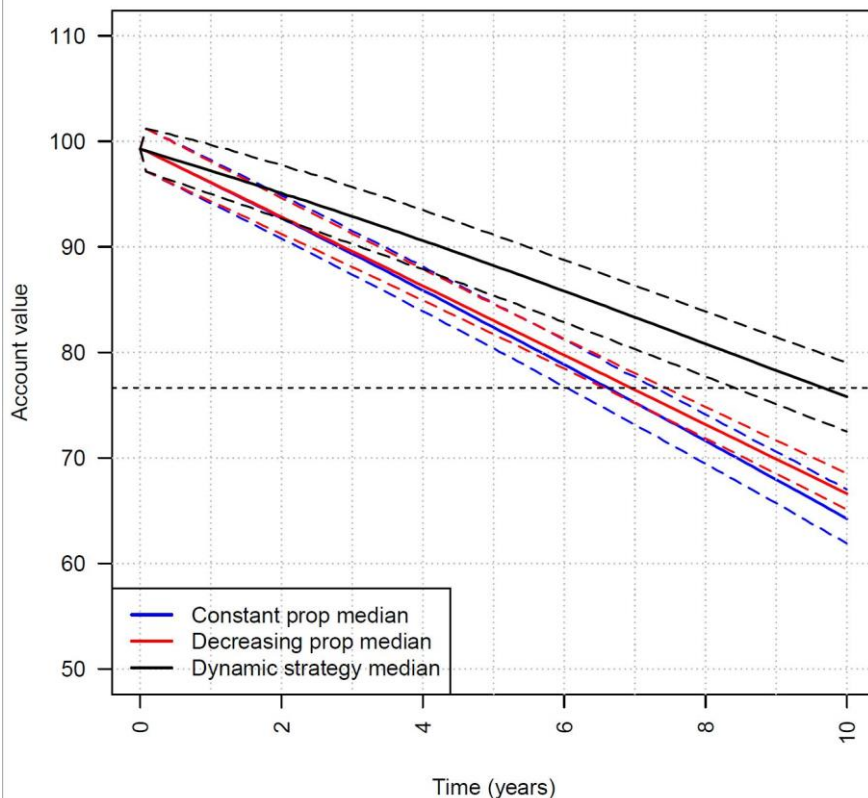
- Median £9.70 p.a. under dynamic strategy,
- +18% higher than constant proportion in risky asset;
- +13% higher than decreasing proportion in risky asset.
- Paid £8.90 p.a. from age 65 to 75.
- Target income was £9.80 p.a. from age 75.



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Improving outcomes: sustainably risk-free income in the first 10 years

Distribution of the PAF account value over time, showing 5th, median and 95th percentiles



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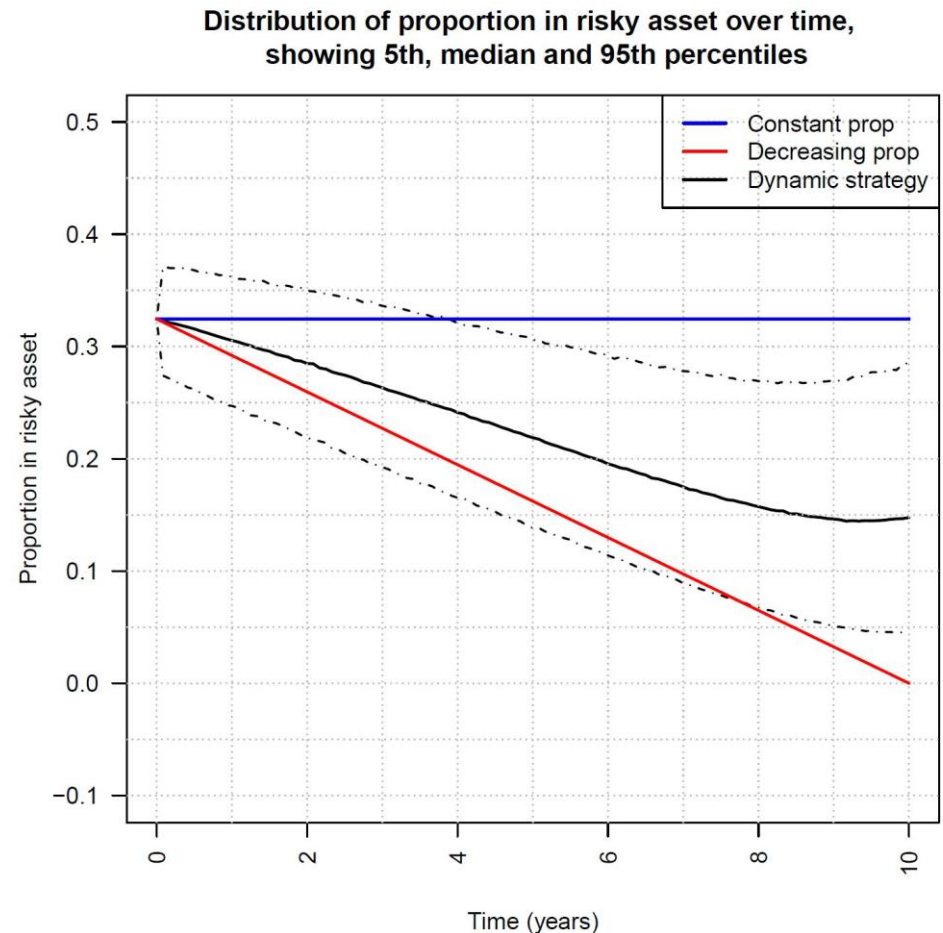
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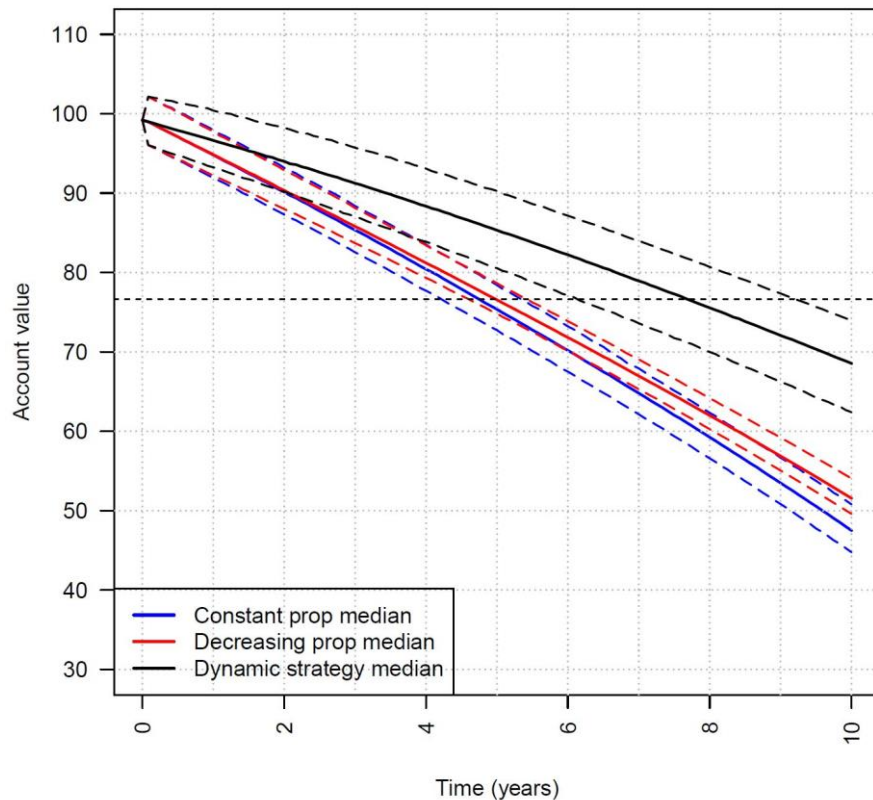
Changing the problem: higher income in the first 10 years

- Would like 10% higher than £8.90 p.a. from age 65 to 75.
- Pay John £9.80 p.a. from age 65 to 75.
- Would like to pay him £9.80 p.a. from age 75 too.



Improving outcomes: higher income in the first 10 years

Distribution of the PAF account value over time,
showing 5th, median and 95th percentiles



Income bought at age 75 is higher under the dynamic strategy:

- Median £8.75 p.a. under dynamic strategy,
- +32-42% higher than other two strategies;
- Median is lower than desired age 75 income (£9.80 p.a.)
- Paying 10% more than age 65 life annuity from age 65 to 75 has noticeable impact.



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Summary

- Pooled annuity fund provides higher income than income drawdown.
 - In the model considered, significantly higher.
- Dynamic investment strategy does better than the two alternatives.
 - Increases risk appetite when fall below the age 75 target annuity value.
 - Decreases risk appetite as approach annuitization time.
- All values are model and problem-dependent!

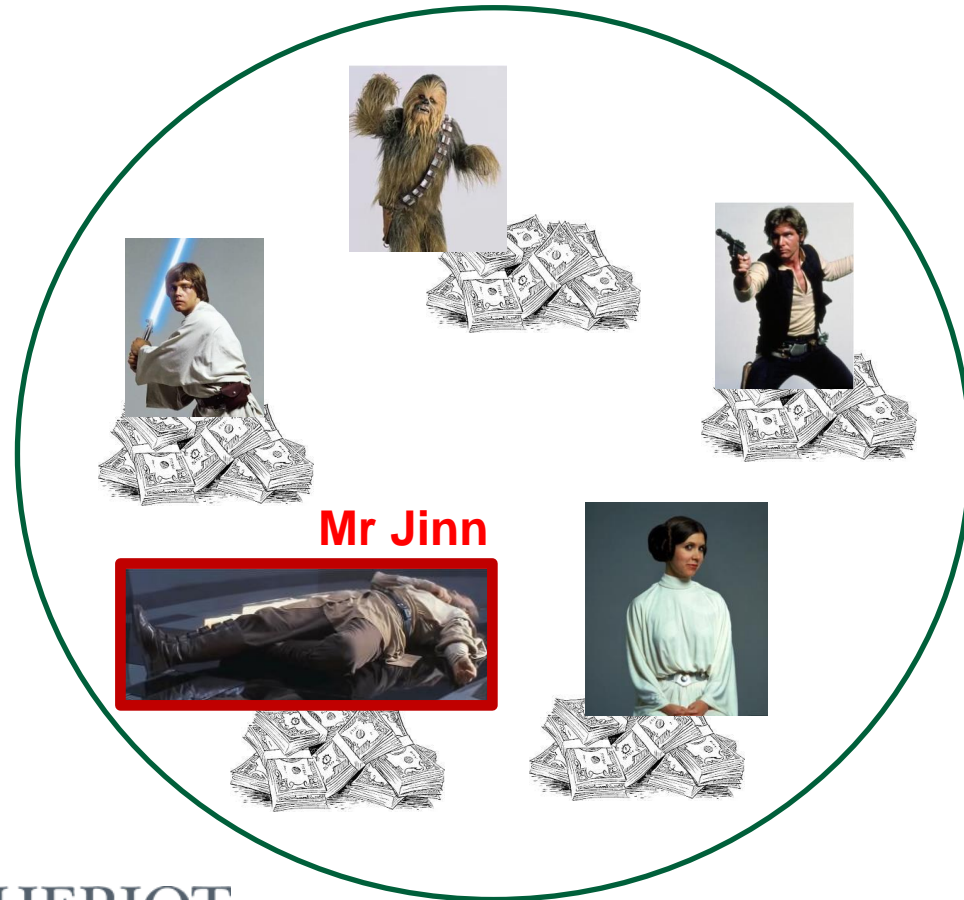


Longevity credit calculation



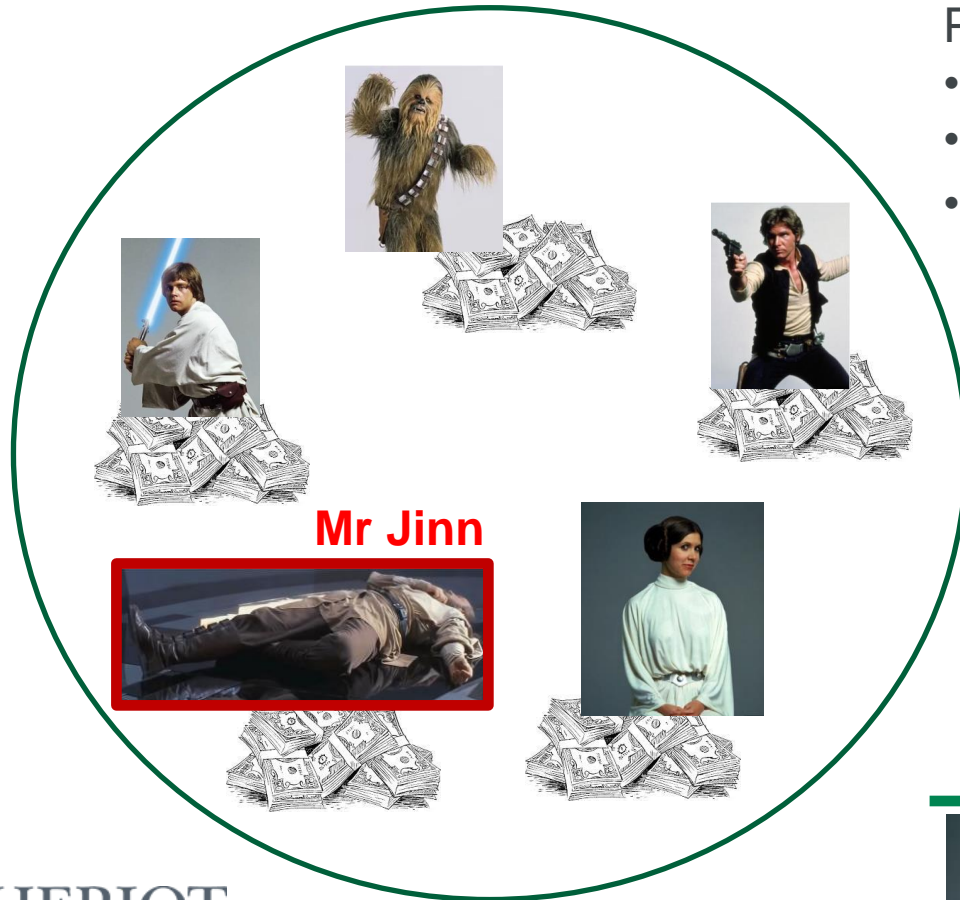
When someone dies during the year, share out their account value among the survivors.

Longevity credit calculation



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Longevity credit calculation



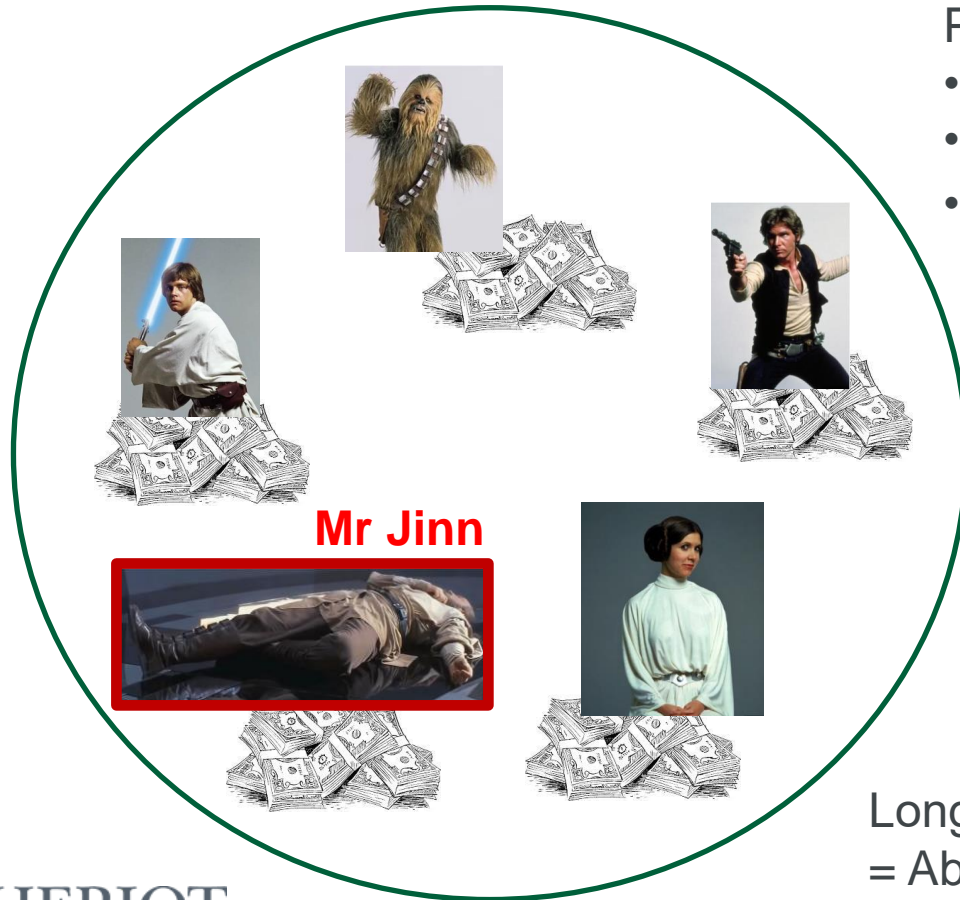
Participant i has:

- Age $x(i)$ at start of year.
- Probability $q_{x(i)}$ of dying over the year.
- Account value F_i at end of the year.

Han Solo's proportional share of Mr Jinn's account value looks like:



Longevity credit calculation



Participant i has:

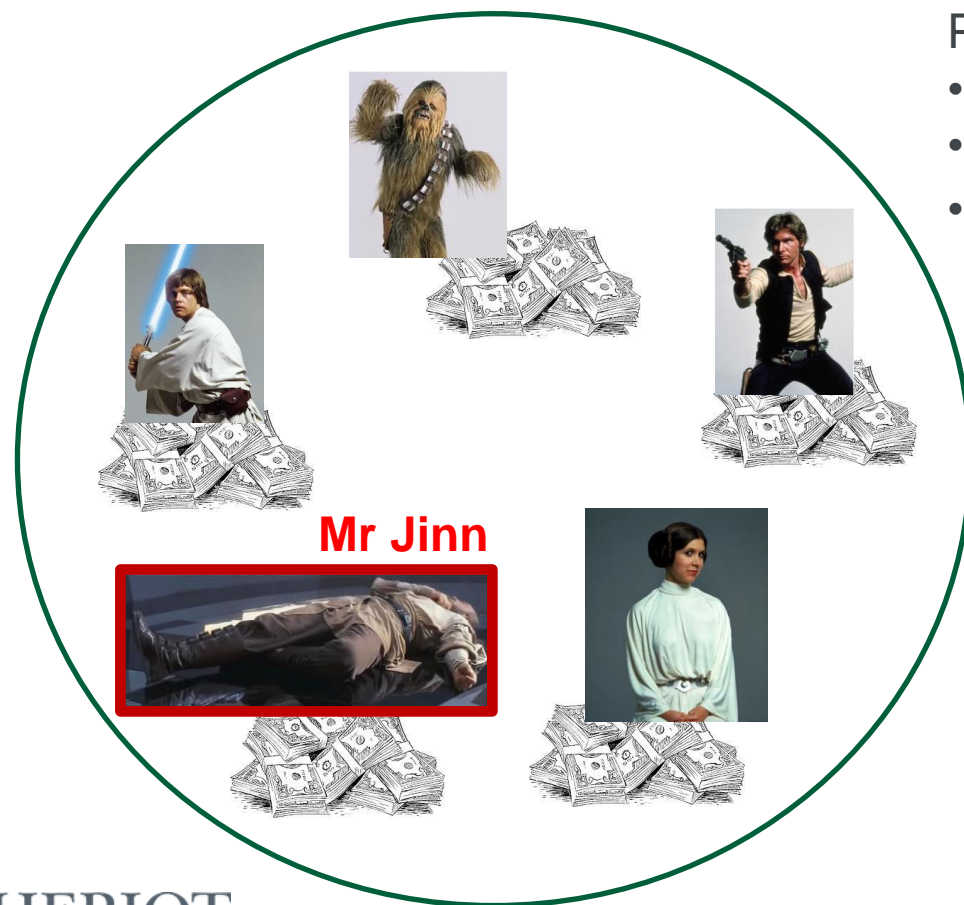
- Age $x(i)$ at start of year.
- Probability $q_{x(i)}$ of dying over the year.
- Account value F_i at end of the year.

Han Solo's (age 80 at start of year) proportional share of Mr Jinn's account value

$$= \frac{\frac{q_{80}}{(1 - q_{80})} \times F_{Han Solo}}{\sum_{Survivors i} \frac{q_{x(i)}}{(1 - q_{x(i)})} \times F_i}$$

Longevity credit paid to Han Solo's account
= Above fraction \times Account value of Mr Jinn.

Longevity credit calculation



Mr Jinn

Participant i has:

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- Probability $q_{x(i)}$ of dying over the year.
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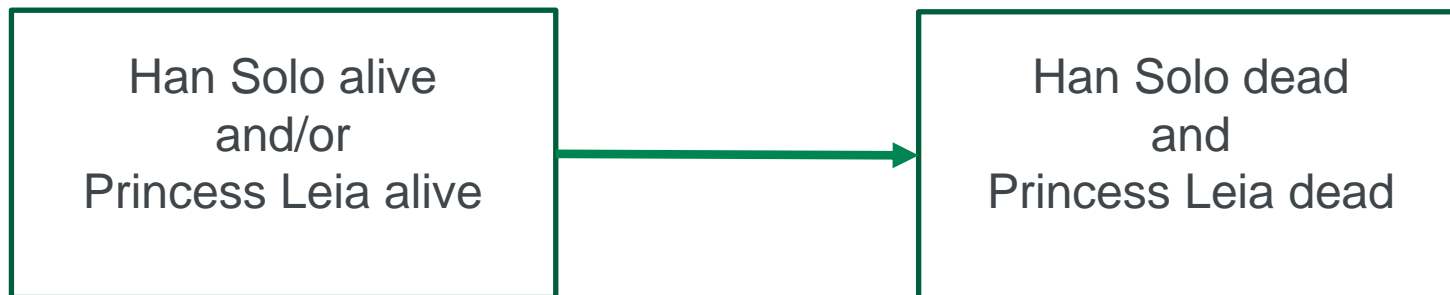
Joint life benefits

- How to pay a joint life benefit? E.g. Pay
 - £100 p.a. while Han Solo and Princess Leia are alive,
 - £50 p.a. if only Han Solo is alive,
 - £50 p.a. if only Princess Leia is alive,
 - Zero if both are dead.
- Reminder of the single life longevity credit calculation...

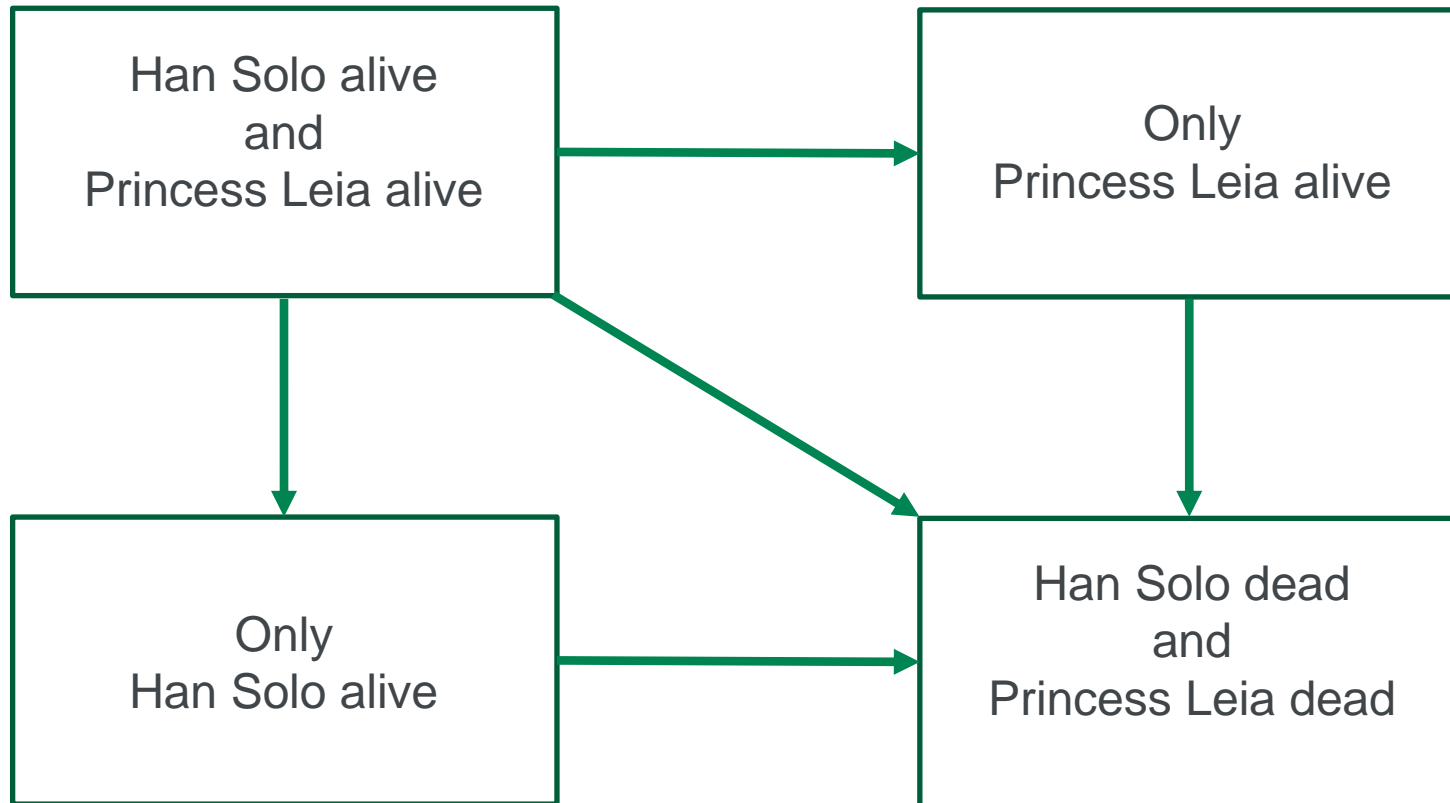
Underlying single life model



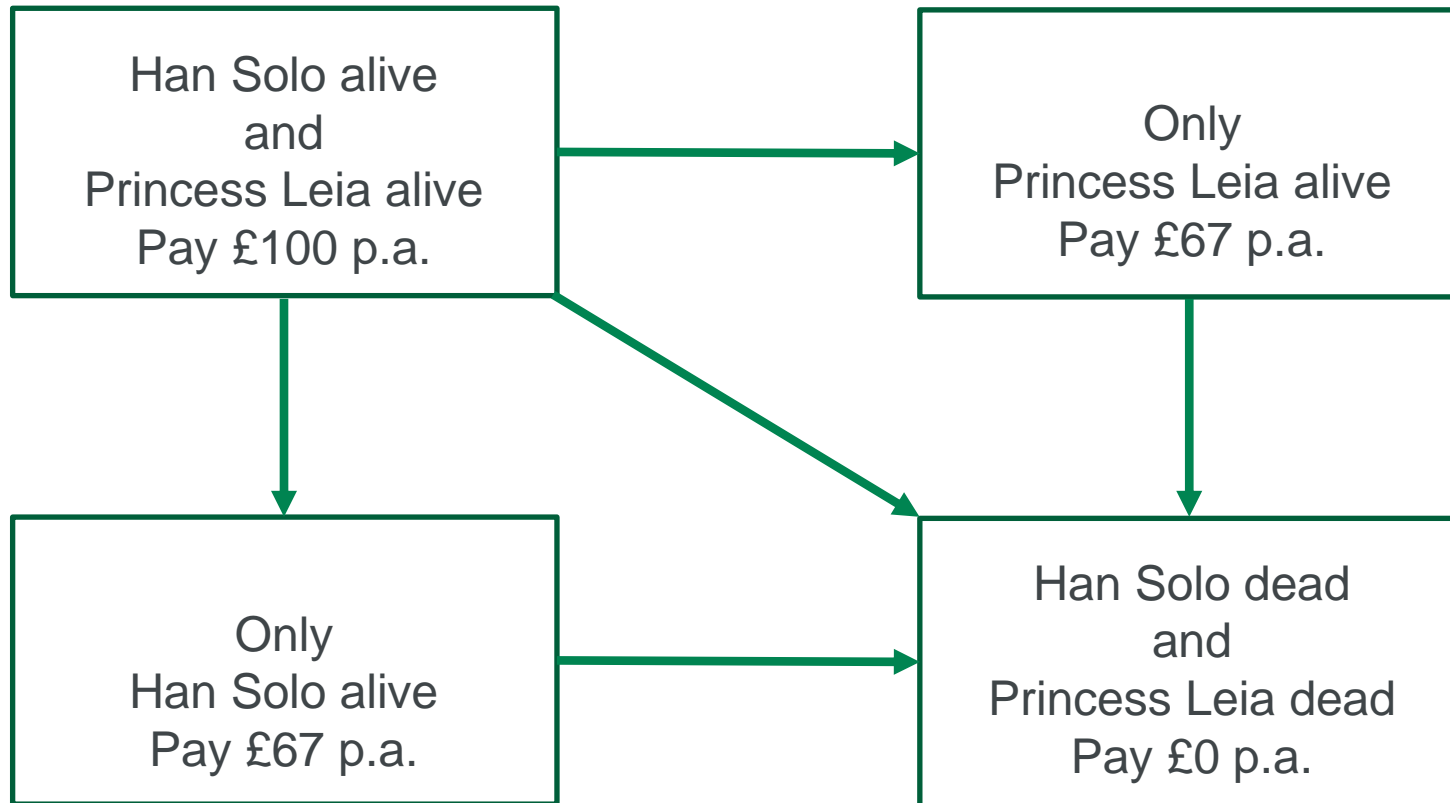
Model for last survivor benefit



Model for joint life benefit



Model for joint life benefit



Calculate the longevity credit in “both alive” state

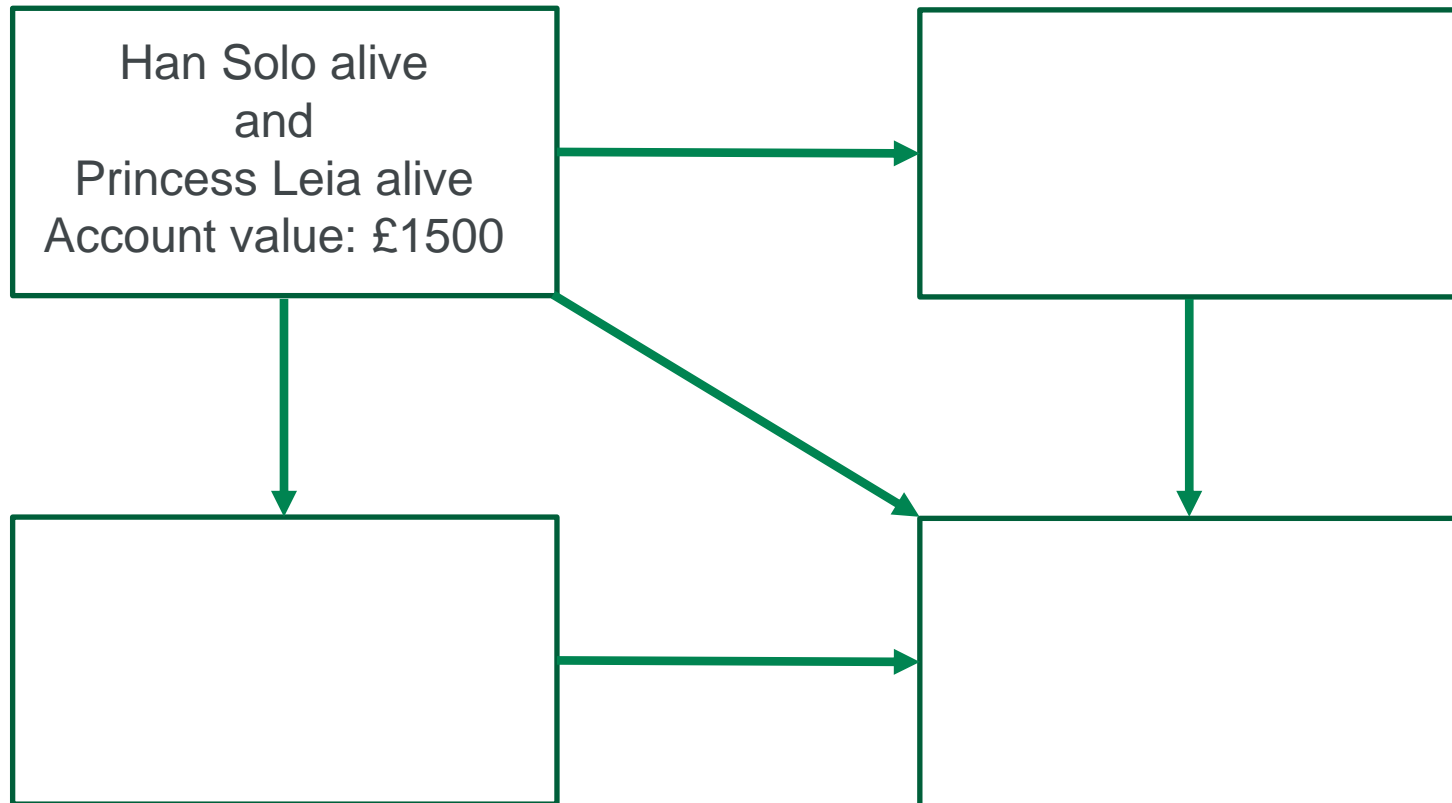
- Shown in ARC paper “Joint Life Income in a Pooled Annuity Fund”.
- What do we see?
- Providing joint life benefits leads to an income-based approach to pooled annuity funds.



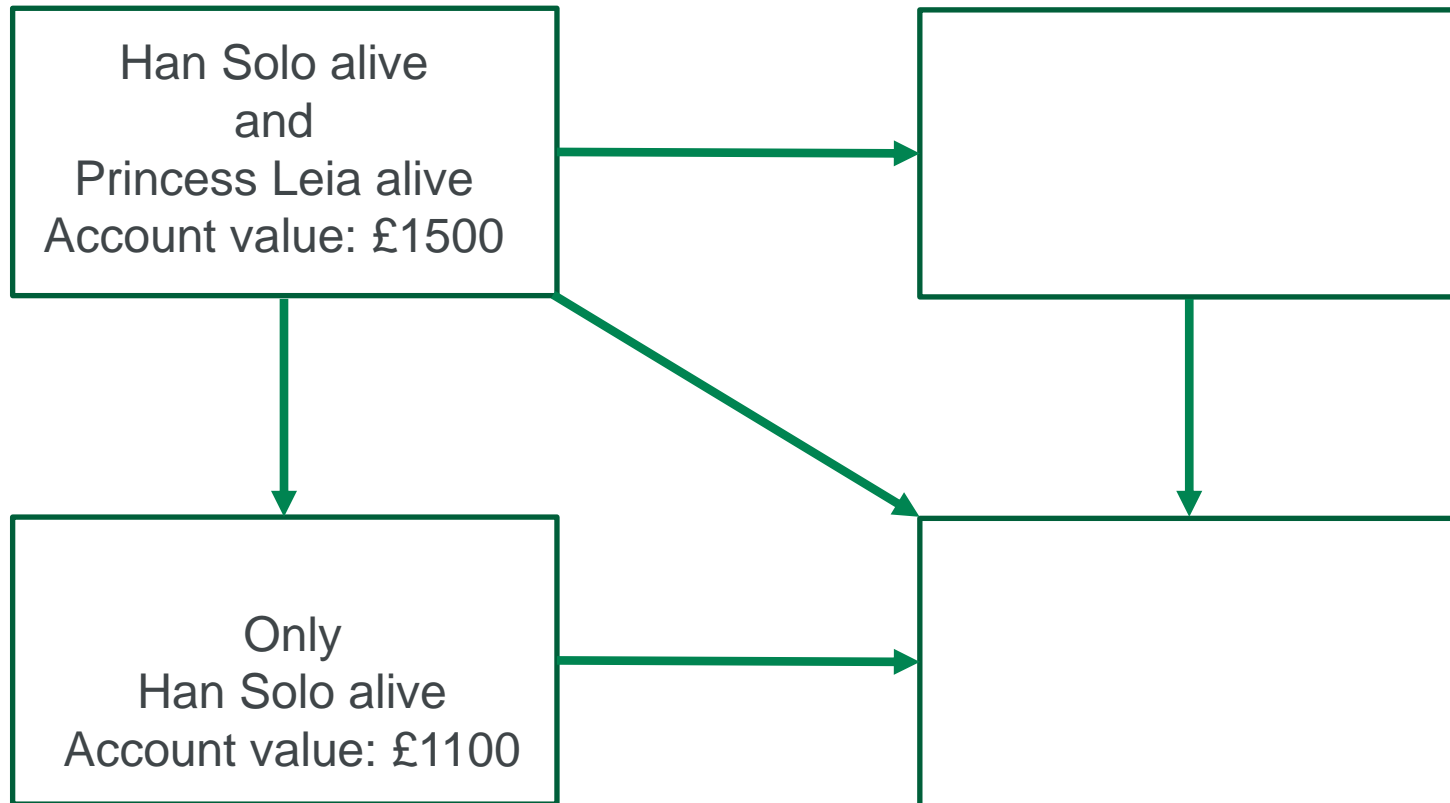
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Model for joint life benefit



Model for joint life benefit



Calculate the longevity credit in “both alive” state

- We see: when one of the couple dies, some of their account value is “lost” ...
- ..It is shared out among the surviving couples.
- Han Solo is left with enough money to provide his widower income and no more!
- Providing joint life benefits leads to an income-based approach....
- ...to avoid unhappy widows/widowers.



Bibliography

- Donnelly, C. and Zhang, X. (2023). “Joint life income in a pooled annuity fund”.
[Found at the IFoA ARC website](#)



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Questions

Comments



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The ARC seeks to deliver cutting-edge research programmes that address some of the significant, global challenges in actuarial science, through a partnership of the actuarial profession, the academic community and practitioners.

The **'Minimising Longevity and Investment Risk while Optimising Future Pension Plans'** research programme is being funded by the ARC.

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