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Critical illness insurance rates: are they changing over time and how?

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Work with
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30 October 2023



www.actuaries.org.uk/arc

Modelling, Measurement and Management of Longevity and Morbidity Risk

- Major research programme funded by the Actuarial Research Centre of the Institute and Faculty of Actuaries running from 2016 to 2020
- Significant supporting funding from the Society of Actuaries and the Canadian Institute of Actuaries
- Themes
 - Development of new single and multi-population models for mortality and new sub-population mortality datasets
 - Drivers of mortality and cause of death analysis
 - Longevity risk management
 - **Stochastic models for critical illness insurance**



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Outline

- Critical illness insurance
- Data
- Stochastic modelling
 - Delay time distribution (diagnosis to settlement)
 - Claim rates
- Claim rates comparison
 - Smoothed rates: 1999-2005 v 2007-2010
- Pricing rates



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Critical illness insurance

Critical illness: Policy description

- Fixed term policy, usually ceasing at age 65
- A fixed sum insured payable on the diagnosis of one of a specified list of critical illnesses
- Covers: Cancer; *Death*; Heart attack; Stroke; Multiple Sclerosis; Total & permanent disability; Coronary artery bypass graft; Kidney failure; Major organ transplant etc.
- Policies are often sold together with term or endowment insurance
- Benefit type: Full Accelerated (FA) or Stand Alone (SA)



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Data

Provided by the CMI Assurances Committee

Data

CII data supplied by CMI:

- 1999-2005
 - Details of policies in force at the start and end of each year
 - 19,000 claims settled
- 2007- 2010
 - Grouped by various risk factors
 - 25,187 claims settled

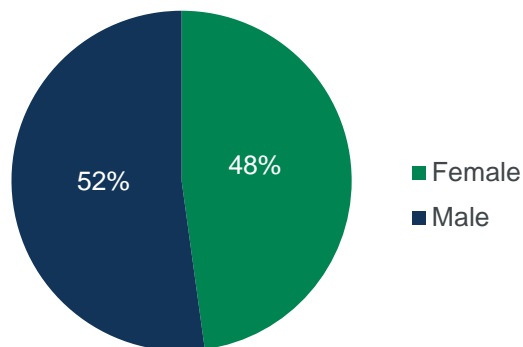
Data:

- Claims
- Exposures
- Risk factors:

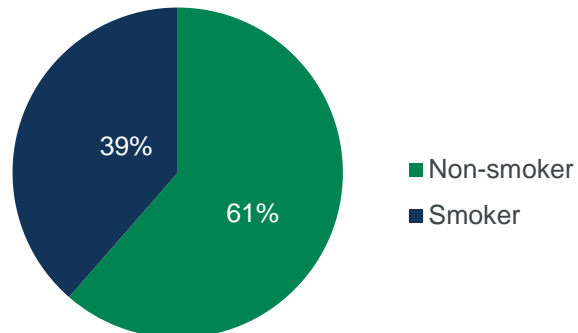
Risk factor (covariate)	1999 – 2005	2007 – 2010
Age (last birthday)	√	√
Gender	√	√
Smoker	√	√
Policy duration	√	√
Office	√	
Distribution channel	√	√
Benefit type (accelerated, standalone)	√	√
Benefit amount	√	√
Policy type (single, joint)	√	
Settlement year	√	√
Cause	√	
Product category		√
Date of diagnosis	√	

Data: 2007 - 2010

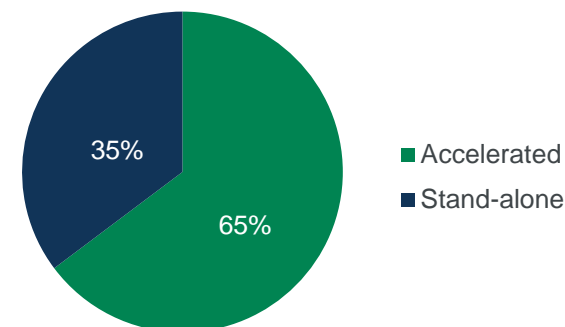
Gender



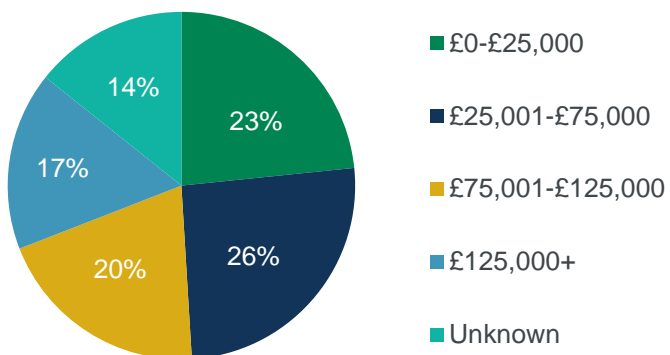
Smoker Status



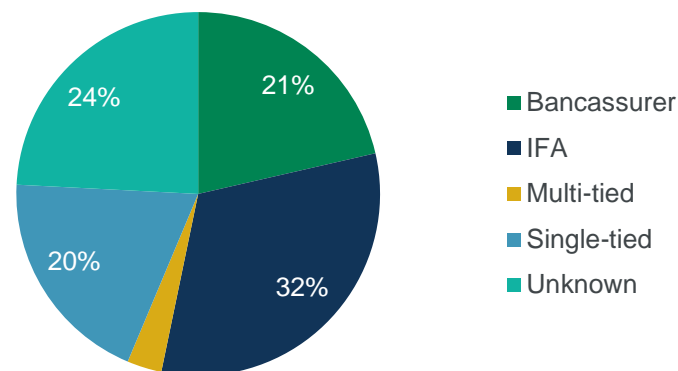
Benefit Type



Sum Assured

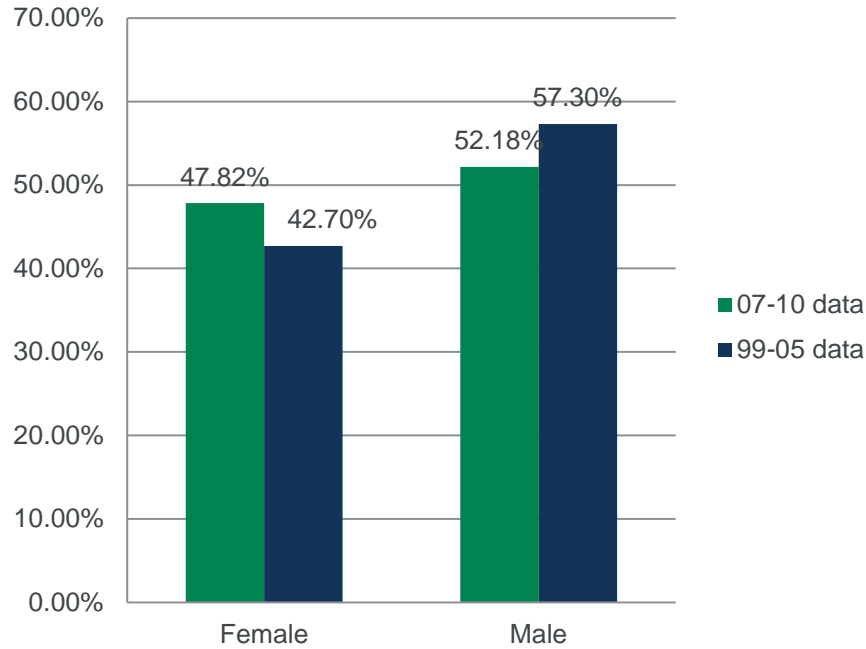


Distribution Channel

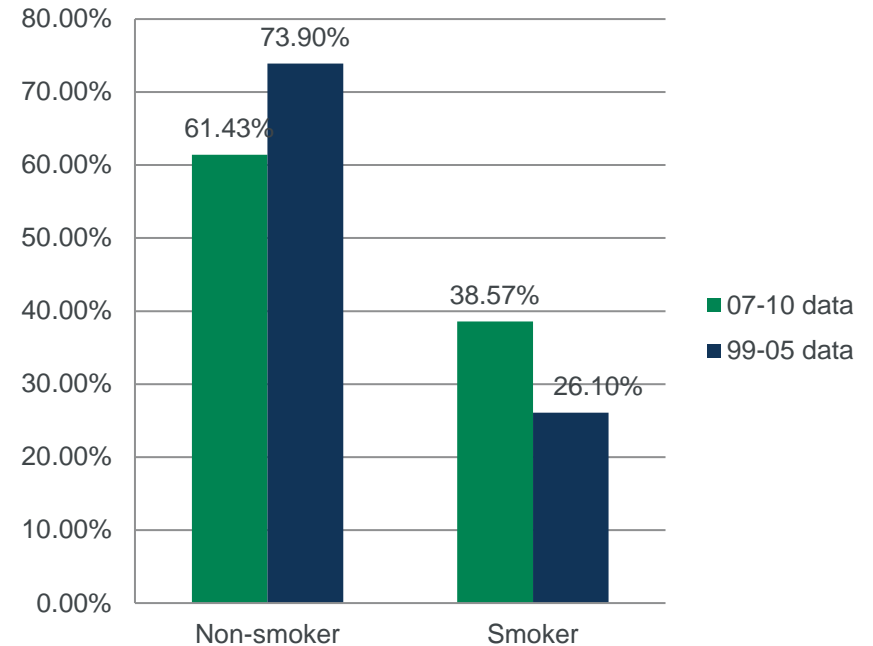


Data: 2007 – 2010 v 1999 – 2005

Gender

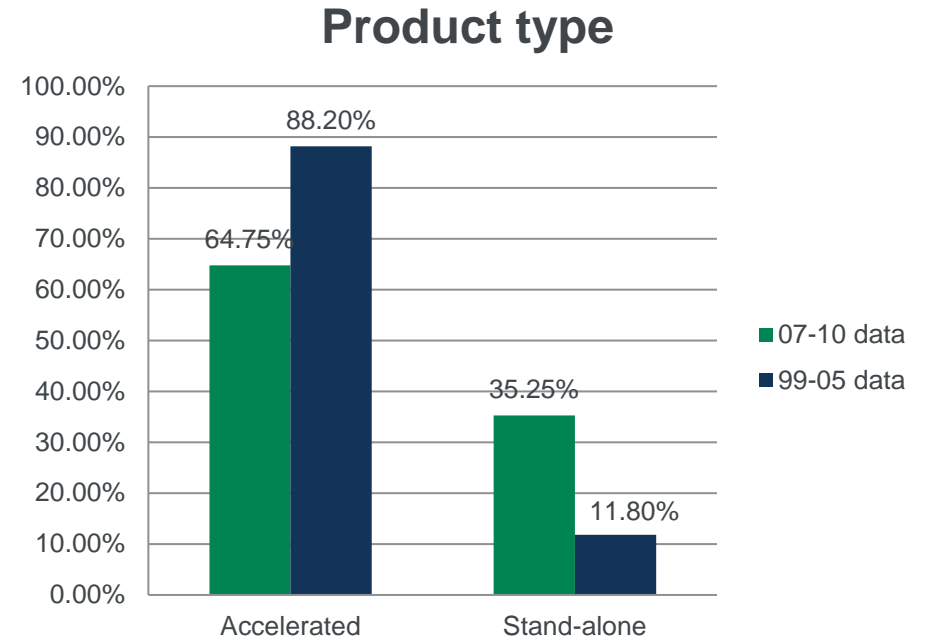
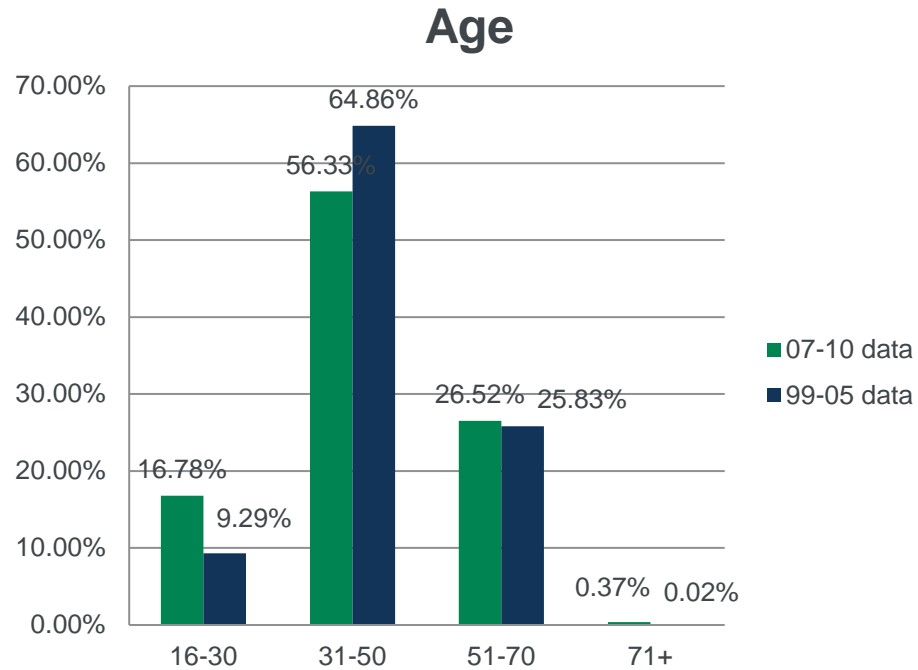


Smoker status



- Distributions more “even” in 2007 – 2010
- Higher proportion of **smokers** in 2007 – 2010

Data: 2007 – 2010 v 1999 – 2005



- Higher proportion of **age 16-30** in 2007 – 2010
- Higher proportion of **stand-alone** in 2007 – 2010



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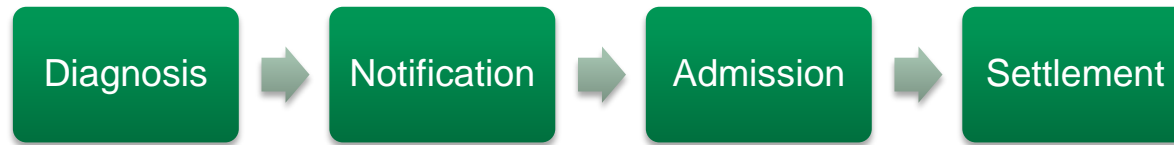
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Modelling

Mostly Bayesian stochastic

Stochastic modelling

- Estimation & smoothing of CI diagnosis rates
 - how do these depend on **risk factors**?
- Diagnosis is the **insured event** and there is a **delay between diagnosis and settlement**



- The **exposure corresponds to claims settled, not to claims diagnosed**
- **This can lead to biased rate estimates; need to adjust it**
- Also take into account uncertainty

Stochastic modelling

Delay time distribution (1999-2005)

- Diagnosis date not always recorded or available
 - 18% diagnosis dates missing
- Observed data: mean delay 185 days; sd 263 days
- Fit a delay distribution (GB2 in Bayesian GLM-type setting):
 - $F(d; x, z) = Pr(\text{claim diagnosed age } x, \text{ risk factors } z, \text{ will be settled in } d \text{ days})$

$D_i \sim \text{Generalised Beta2}(\alpha, \tau, \gamma, s_i)$

$$f_D(d_i) = \frac{\Gamma(\alpha + \gamma)}{\Gamma(\alpha)\Gamma(\gamma)} \frac{\tau (d_i/s_i)^{\tau\gamma}}{d_i [1 + (d_i/s_i)^\tau]^{\alpha+\gamma}}$$

$$E(D_i) = \exp(\eta_i) = \exp\left(\beta_0 + \sum_{j=1}^8 \beta_j z_{ij} + \beta_{9,k} + \beta_{10,l}\right)$$

with s_i given as function of $\eta_i, \alpha, \tau, \gamma$.



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Stochastic modelling

Delay time distribution (1999-2005)

- Most factors significant:
 - Policy duration, amount, death: **shorter delay**
 - Single life, stroke, multiple sclerosis: **longer delay**
- Non-recorded **diagnosis dates estimated through delay distribution $F()$**
- Data (exposures) adjusted to allow for non-settled claims

$$E^*(u; x) = E(u; x) \times F(t-u; x)$$

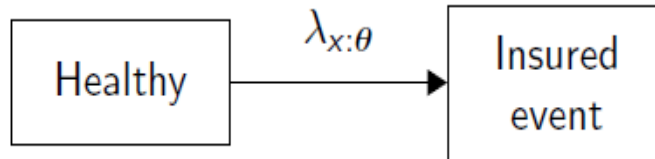
Stochastic modelling

Delay time distribution (2007 – 2010)

- Diagnosis date **not available**
- Assume similar delay distribution
- Match claims with common characteristics (age, policy duration etc)
- Adjust exposures as in earlier data

Stochastic modelling: Claim rates

Model:



Fit Bayesian model:

$$N^{(j)}(x; \theta) \sim \text{Poisson} \left(\lambda_{x; \theta}^{(j)} \int_{u=0}^4 E(u : x; \theta) F^{(j)}(4 - u : x; \theta) du \right)$$

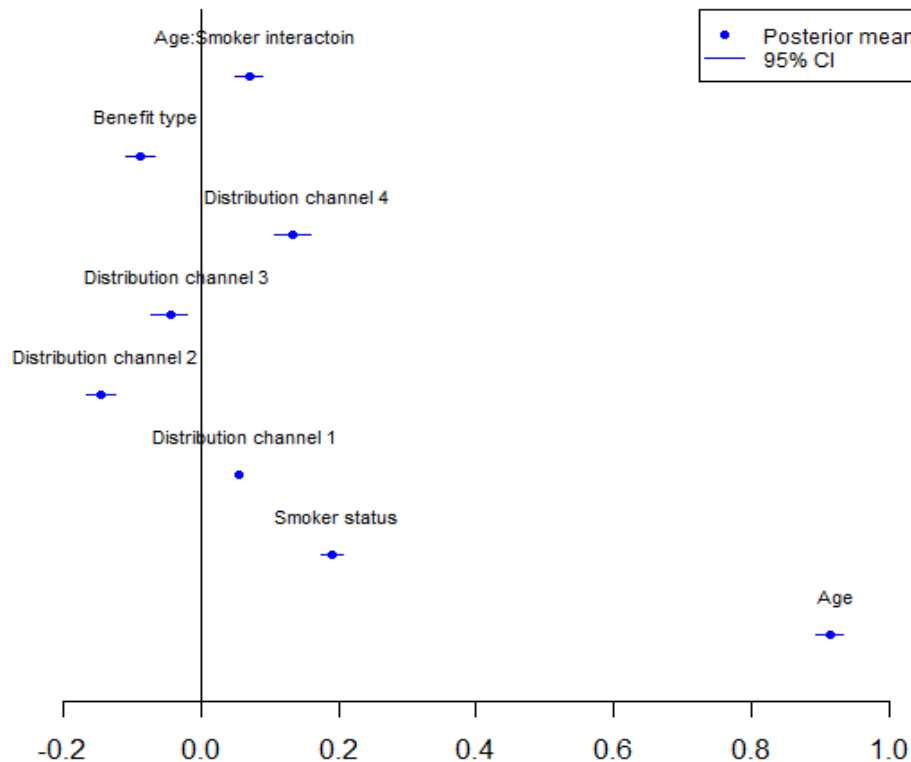
Adjusted exposure

- $\lambda_{x, \theta}^{(j)}$: **diagnosis (claim) rate** for cause j at age x with risk factors θ

Stochastic modelling:

Risk factor estimates for claim rates (2007 – 2010)

Risk factors: Bayesian estimates



Perform variable (factor) selection

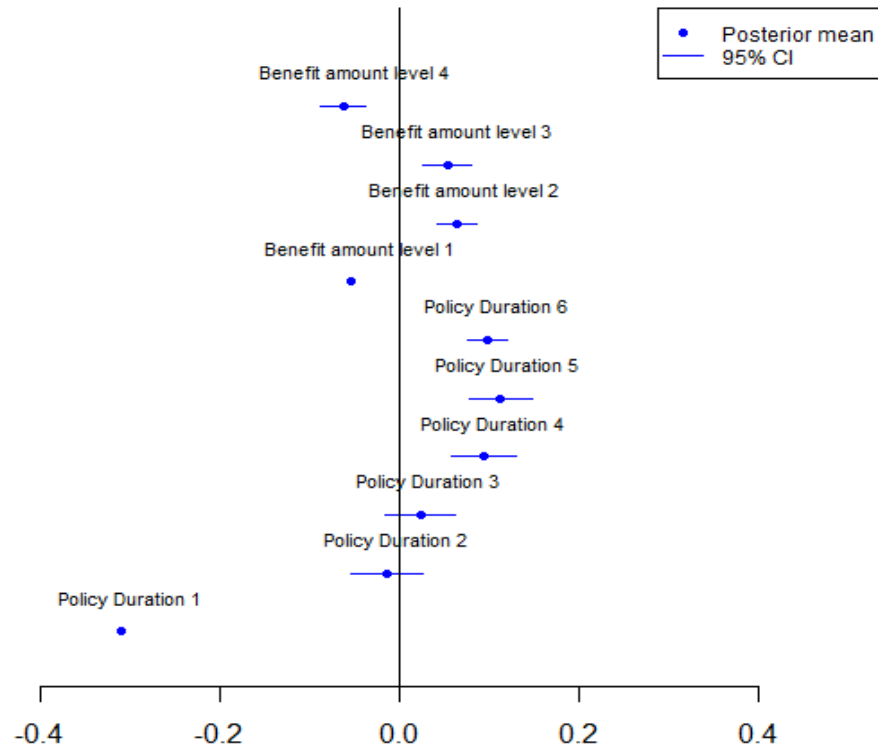
Selected model includes:

- ✓ age (older ↑)
- ✓ smoker status (S ↑)
- ✓ distribution channel
- ✓ benefit type (stand-alone ↓)
- ✓ age x smoker

Stochastic modelling:

Risk factor estimates for claim rates (2007 – 2010) cont.

Risk factors: Bayesian estimates



Selected model includes:

- ✓ policy duration (longer ↑)
- ✓ benefit amount (mid ↑)



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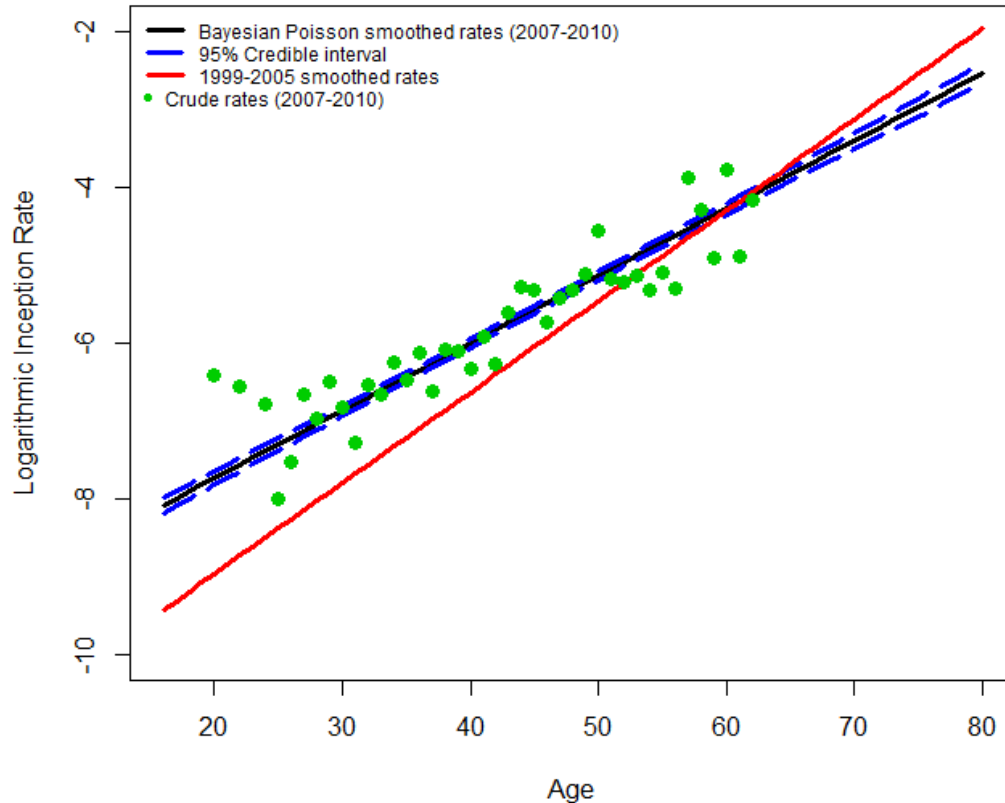
Claim rates

Smoothed estimates, intervals

Claim rates

2007-2010 v 1999 – 2005, Accelerated, Smoker, Pol Duration 1

Logarithmic inception Rate for FA type
Smoker with PoIDur 1

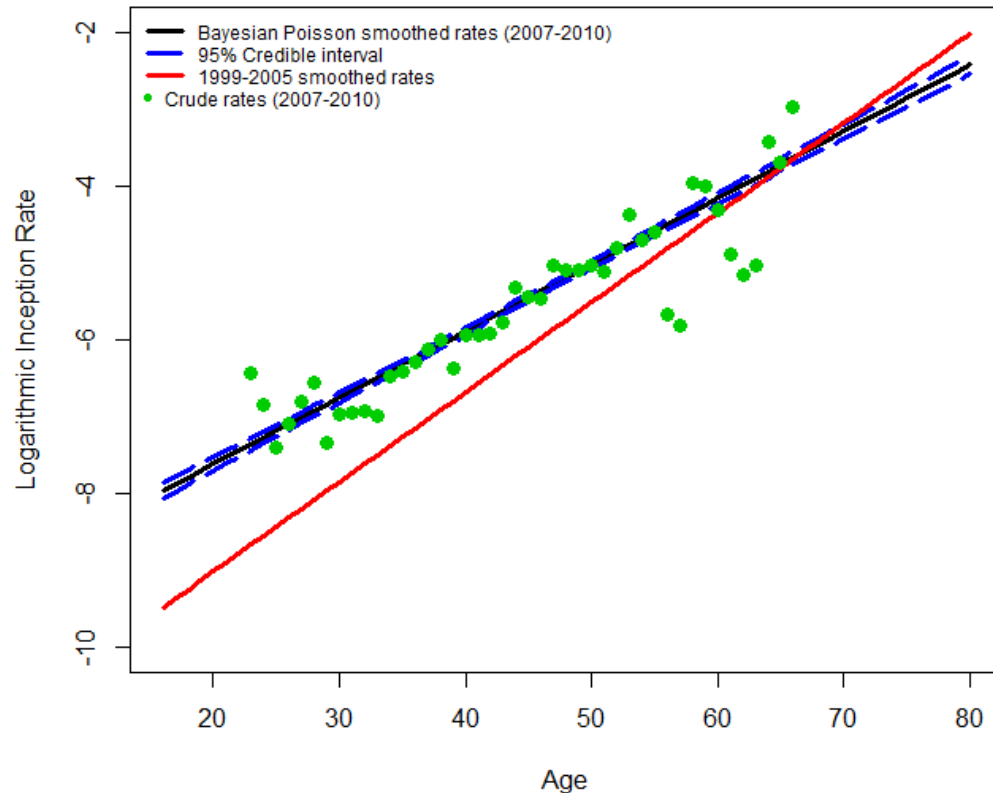


- ❖ Model fits crude rates (2007 – 2010) well
- ❖ 2007 – 2010 rates significantly higher
- ❖ Gap widens at younger ages

Claim rates

2007-2010 v 1999 – 2005, Accelerated, Smoker, *Pol Duration 4*

Logarithmic Inception Rate for FA type
Smoker with PolDur 4

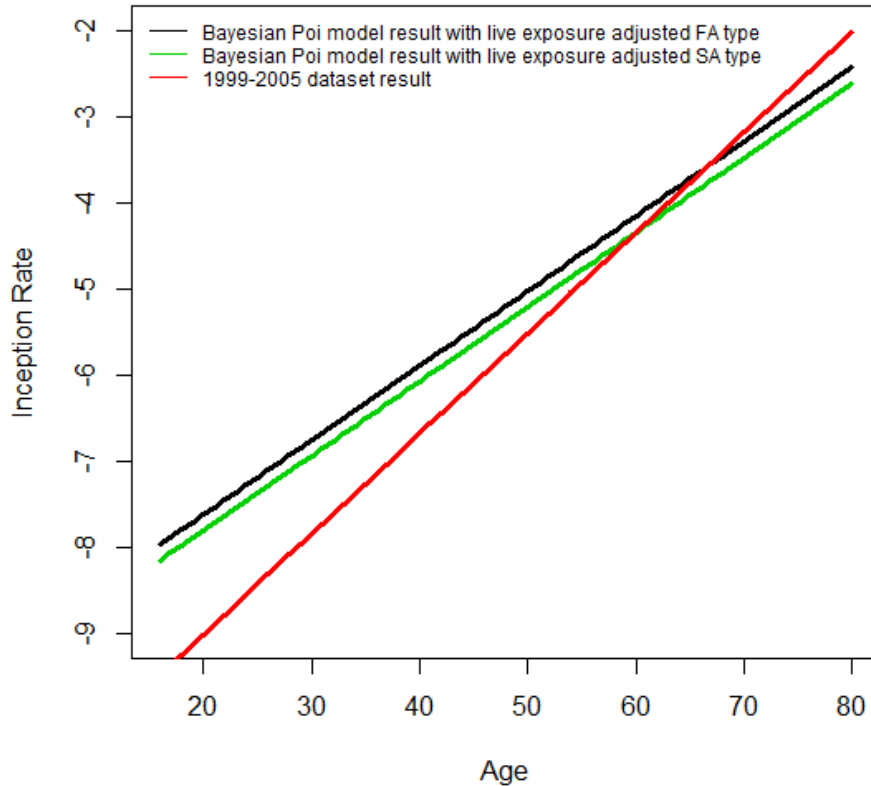


- ❖ Again, 2007 – 2010 rates significantly higher
- ❖ Rates higher than for Pol Duration 1

Claim rates

Accelerated v Stand alone (2007 – 2010) & 1999 – 2005

Inception Rate for Different Benefit type
Smoker with PoIDur 4

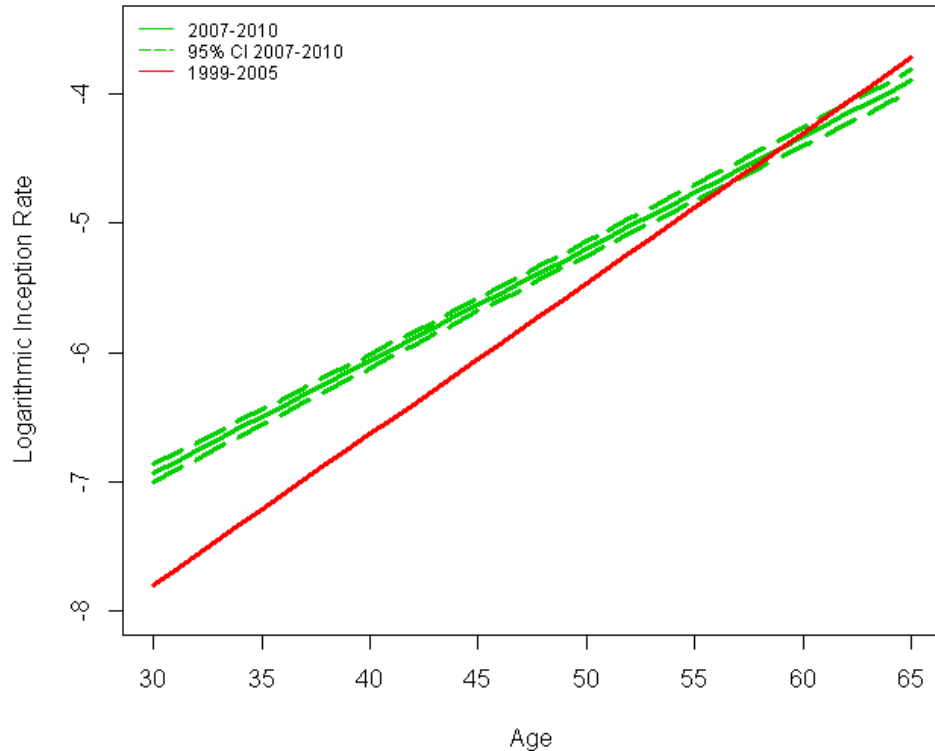


- ❖ Accelerated 2007 -2010 (black) higher than stand-alone (green)
- ❖ Both significantly higher than 1999 – 2005

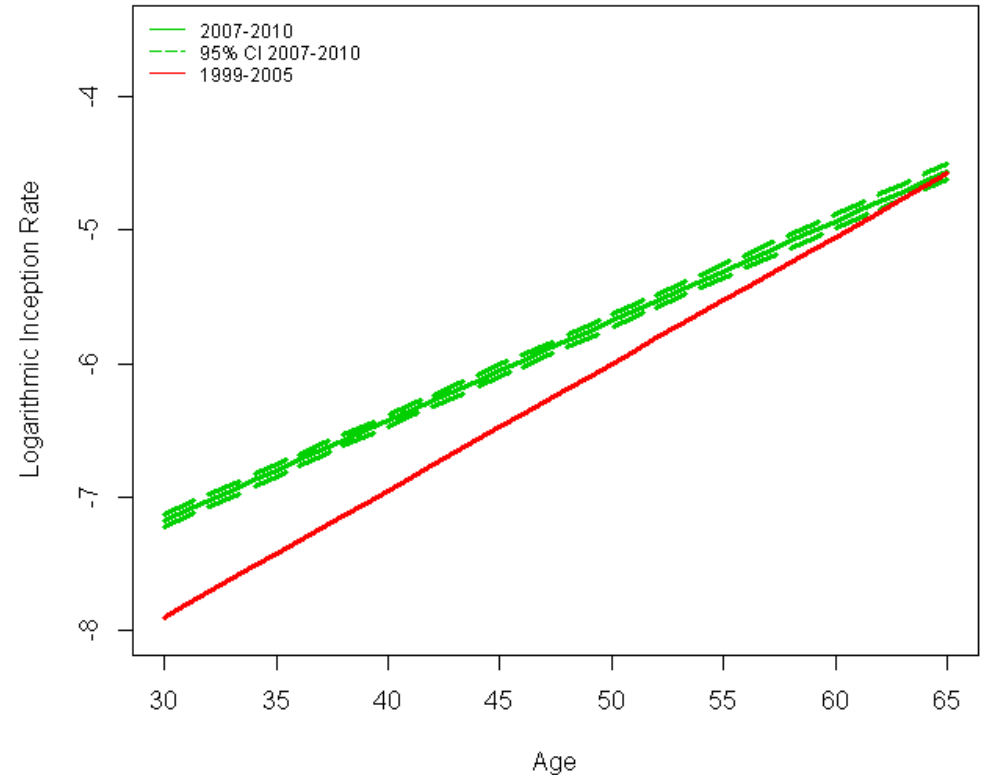
Claim rates

Smokers & non-smokers (Accelerated, Pol Duration 1)

Inception rates, FA, PolDur 1
Smokers



Inception rates, FA, PolDur 1
Non-smokers

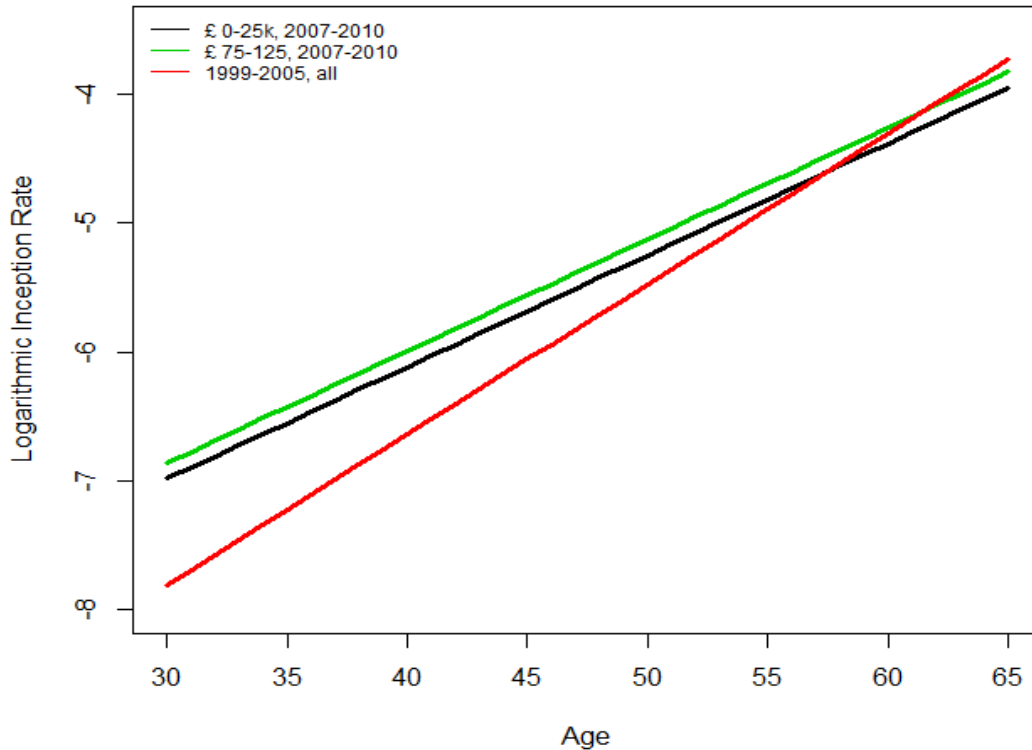


❖ 2007 – 2010 rates significantly higher, both S & NS

Claim rates

Different benefit amount (Accelerated, Smokers)

Inception rates, FA, smokers
different benefit amount



- ❖ 2007 – 2010 rates significantly higher, also for different amount



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Pricing

Pricing

Annual premium, paid at constant rate, n-year term:

$$\text{Net Premium} = \text{Benefit Amount} \times \frac{\int_{t=0}^n v^t {}_t p_x \lambda_{x+t} dt}{\int_{t=0}^n v^t {}_t p_x dt}$$

where

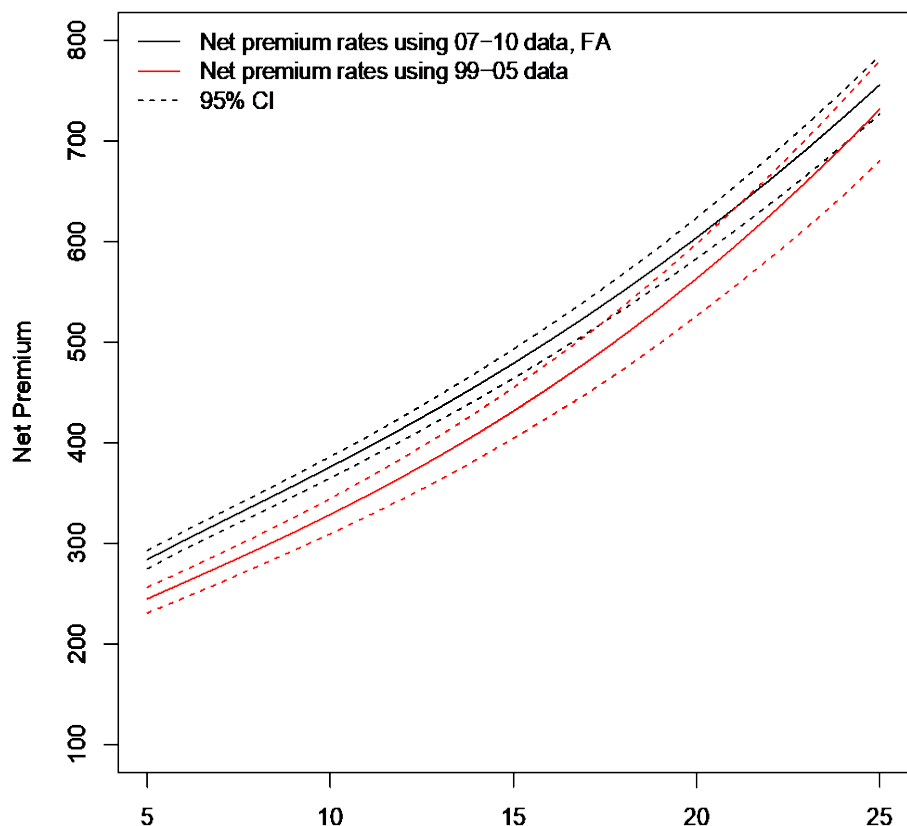
$${}_t p_x = \exp\left(-\int_{s=0}^t \lambda_{x+s} dt\right) \text{ and}$$

v is the discount factor.

Then bootstrap distribution of λ s used to derive CIs for premiums.

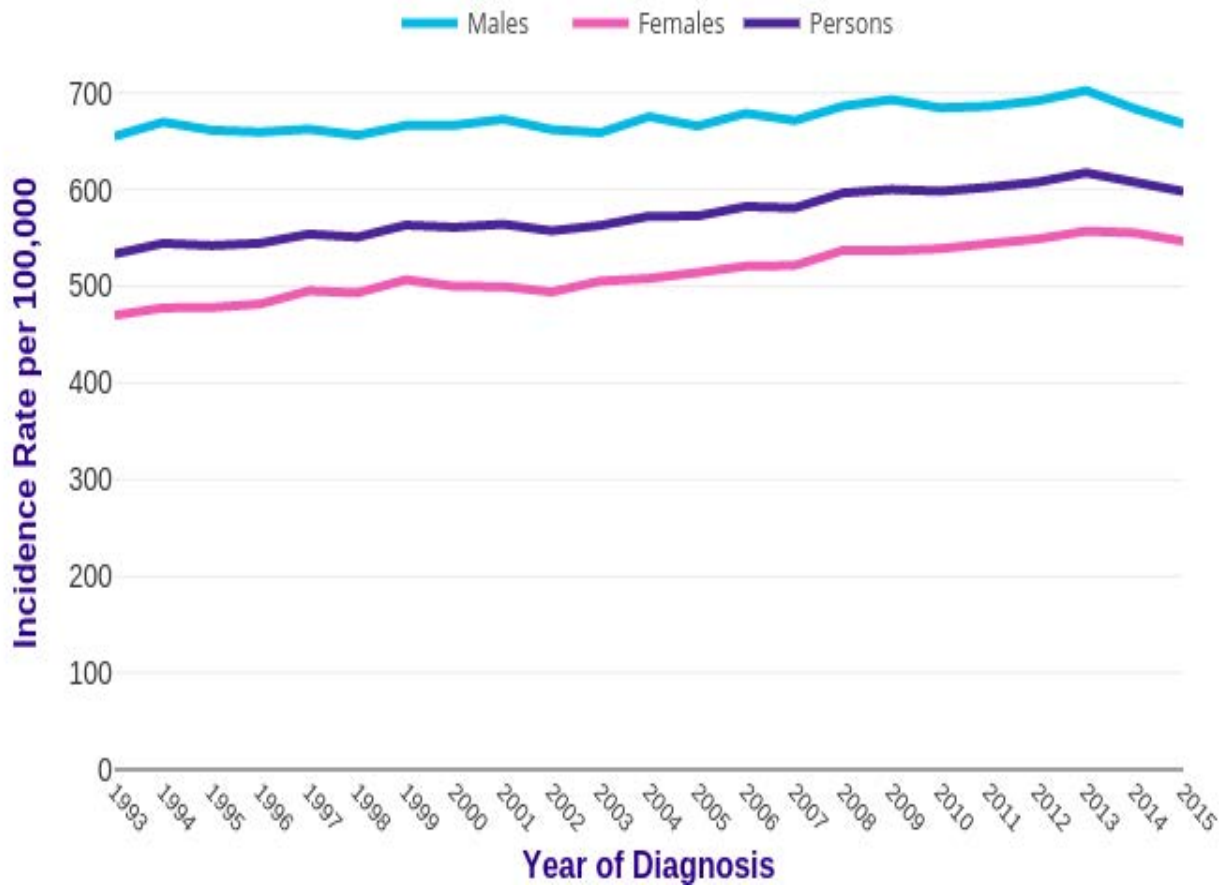
Pricing

All causes, Smoker, Age 40, Policy duration 0, Benefit amount £100k, $i=3\%$



- ❖ Since 2007 – 2010 FA rates are higher than 1999-2005 combined rates, the net premium rates are also higher.

All Cancers Excluding Non-melanoma Skin Cancer (UK)



In 1999-2005 dataset

- ❖ 49% of the claims were caused by cancer
- ❖ Death 17.6%
- Heart attack 11.6%
- CABG 2.1%

Source: cruk.org/cancerstats



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Future trends of CII claims

- Cancer forms almost half of the CII claims.
 - Availability of screening (e.g. colonoscopy, mammography)
 - Social/behavioural changes (e.g. obesity, alcohol consumption)
 - New treatments (e.g. targeted immunotherapy)
 - Statistical advances (e.g. use of big data, AI methods)



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Conclusions

Conclusions

- Critical illness insured population distribution has some differences between 1999-2005 & 2007-2010
- Time between diagnosis and settlement of a claim is important
- Claim rates (2007-2010) depend on a number of risk factors including:
 - age, smoker status, distribution channel, policy duration, benefit amount and benefit type
- Analysis suggests increase of a CII claim and premium rates over time (1999-2005 v 2007-2010)
 - especially at younger ages

Continuing work

- Fit more sophisticated Bayesian model to allow for more variation in rates (e.g. hierarchical, negative binomial)
- Use of population morbidity statistics
- Liaise with CMI for knowledge exchange on data, modelling
- Compare with CMI rates

Questions

Comments

The views expressed in this presentation are those of the presenter.

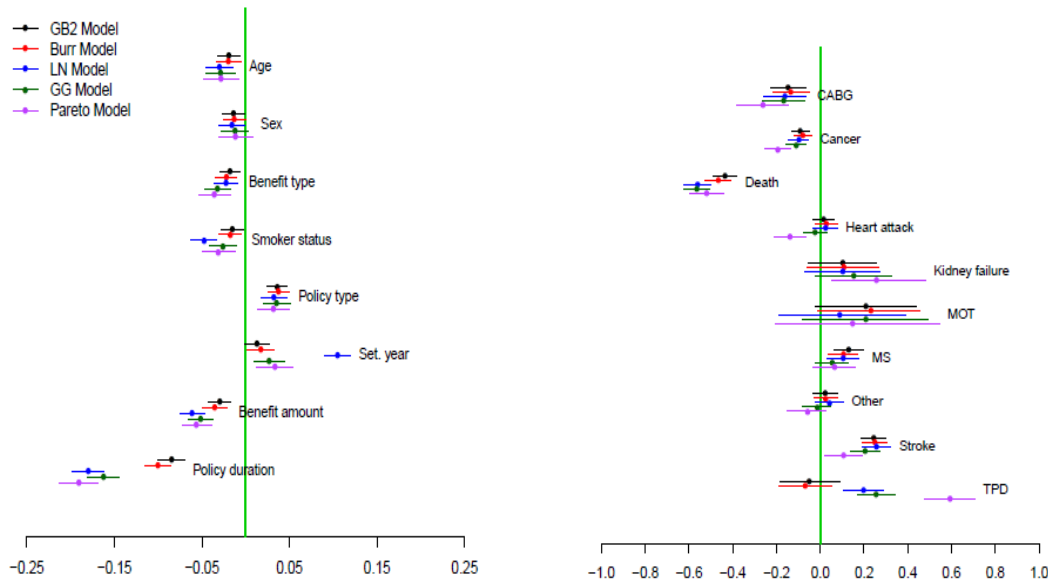


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Stochastic modelling: Delay time distribution

1999 – 2005 (cont.)

- Generalised Beta 2 distribution in Bayesian GLM-type setting



Most factors significant:

- Policy duration, amount, death, CABG: **shorter** delay
- Single life, stroke, mult sclerosis: **longer** delay

Figure: Posterior means (dots) and 95% credible intervals (bars) of β 's.